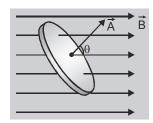
# **ELECTRO MAGNETIC INDUCTION**

# 1. INTRODUCTION

In year 1820 Orested discovered the magnetic effect of current. Faraday gives the thought that reverse of this phenomenon is also possible i.e. current is also produced by magnetic field. Faraday threw a magnet in a coil which is connected by a sensitive galvanometer when the magnet passes through the coil the galvanometer gives instantaneous deflection.

# Magnetic Flux

The magnetic flux ( $\phi$ ) linked with a surface held in a magnetic field (B) is defined as the number of magnetic field lines crossing that area (A). If  $\theta$  is the angle between the direction of the field and normal to the area, (area vector) then  $\phi = \vec{B}.\vec{A} = BA\cos\theta$ 



# • Flux Linkage

If a coil has more than one turn, then the flux through the whole coil is the sum of the fluxes through the individual turn.

If the magnetic field is uniform, the flux through one turn is  $\phi = BA \cos\theta$ 

If the coil has N turns, the total flux linkage  $\phi = NBA \cos\theta$ 

• Magnetic field lines are imaginary, magnetic flux is a real scalar physical quantity with dimensions

$$[\phi] = B \times area = \left[\frac{F}{IL}\right][L^2] \qquad [\because F = B \ I \ L \ sin\theta] \qquad \therefore \ [\phi] = \left[\frac{ML \ T^{-2}}{AL}\right][L^2] = [ML^2 \ T^{-2} \ A^{-1}]$$

### • SI unit of magnetic flux φ

: [M L<sup>2</sup> T<sup>-2</sup>] corresponds to energy

$$\frac{joule}{ampere} = \frac{joule \times sec}{coulomb} = weber (Wb) or T-m^2 (as tesla = Wb/m^2)$$

**CGS UNIT of magnetic flux \phi:** maxwell (Mx),  $1\text{Wb} = 10^8 \text{ Mx}$ 

# **GOLDEN KEY POINTS**

• For a given area flux will be maximum:

when magnetic field  $\overset{
ightharpoonup}{B}$  is normal to the area (transverse field)

$$\theta = 0^{\circ} \implies \cos \theta = \text{maximum} = 1$$

$$\phi_{\text{max}} = B A$$

For a given area flux will be minimum :

when magnetic field  $\overset{\rightarrow}{B}$  is parallel to the area (longitudinal field)

$$\theta = 90^{\circ}$$
  $\Rightarrow$   $\cos\theta = 0$   $\phi_{min} = 0$ 







# Illustrations

### Illustration 1.

A rectangular loop of area 0.06 m<sup>2</sup> is placed in a magnetic field 1.2 T with its plane inclined 30° to the field direction. Find the flux linked with plane of loop.

### **Solution:**

B = 1.2 T and  $\theta = 90^{\circ} - 30^{\circ} = 60^{\circ}$ Area of loop  $A = 0.06 \text{ m}^2$ ,

So, the flux linked with the loop is  $\phi = BA \cos\theta = 1.2 \times 0.06 \times \cos 60^{\circ} = 1.2 \times 0.06 \times 1/2 = 0.036$  Wb

### Illustration 2.

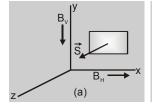
A loop of wire is placed in a magnetic field  $\vec{B} = 0.3\hat{j}T$ . Find the flux through the loop if area vector is  $\vec{A} = (2\hat{i} + 5\hat{i} - 3\hat{k})m^2$ 

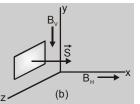
### **Solution:**

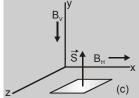
 $\vec{B} = (0.2\hat{i} + 0\hat{j} + 0\hat{k})$  Flux linked with the surface  $\phi = \vec{B} \cdot \vec{A} = (0.3\hat{j}) \cdot (2\hat{i} + 5\hat{j} - 3\hat{k})m^2 = 1.5$  Wb

# Illustration 3.

At a given plane, horizontal and vertical components of earth's magnetic field  $B_H$  and  $B_V$  are along x and y axes respectively as shown in figure. What is the total flux of earth's magnetic field







associated with an area S, if the area S is in (a) x-y plane (b) y-z plane and (c) z-x plane.

### **Solution:**

$$\overrightarrow{B} = \hat{i} B_{u} - \hat{j} B_{v} = \text{constant},$$
 so

$$\phi = \overrightarrow{B} \cdot \overrightarrow{S}$$

$$\phi = \overrightarrow{B} \cdot \overrightarrow{S}$$
 [ $\overrightarrow{B}$  = constant]

(a) For area in x-y plane 
$$\vec{S} = S\hat{k}$$

$$\phi_{xy} = (\hat{i} B_H - \hat{j} B_V).(\hat{k}S) = 0$$

$$\text{(b)} \qquad \text{For area S in y-z plane } \ \overset{\rightarrow}{S} = S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = B_H \, S \, \hat{i} \qquad \qquad \phi_{yz} = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, S) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V). \\ (\hat{i} \, B) = (\hat{i} \, B_H - \hat{j} \, B_V).$$

$$\phi_{yz} = (\hat{i} B_H - \hat{j} B_V).(\hat{i} S) = B_H S$$

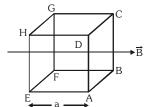
(c) For area S in z-x plane 
$$\vec{S} = S\hat{j}$$

$$\phi_{zx} = (\hat{i} B_H - \hat{j} B_V).(\hat{j} S) = -B_V S$$

Negative sign implies that flux is directed vertically downwards.

# **BEGINNER'S BOX-1**

- 1. A coil of 100 turns, 5cm<sup>2</sup> area is placed in external magnetic field of 0.2 Tesla (S.I.) in such a way that it makes an angle 30° with the field direction. Calculate magnetic flux through the coil (in weber).
- 2. A coil of N turns, A area is placed in uniform transverse magnetic field B. If it is turn through 180° about its one of the diameter in 2 seconds. Find rate of change of magnetic flux through the coil.
- 3. A square cube of side 'a' is placed in uniform magnetic field 'B'. Find magnetic flux through each face of the cube .



- 4. The magnetic field perpendicular to the plane of a loop of area 0.1 m<sup>2</sup> is 0.2 T. Calculate the magnetic flux through the loop.
- The magnetic field in a certain region is given by  $\vec{B} = (4\hat{i} \hat{k})$  tesla. How much magnetic flux passes through 5. the loop of area  $0.1 \text{m}^2$  in this region if the loop lies flat in xy plane?
- 6. A solenoid 4cm in diameter and 20cm in length has 250 turns and carries a current of 15A. Calculate the flux through the surface of a disc of 10cm radius that is positioned perpendicular to and centered on the axis of the solenoid.

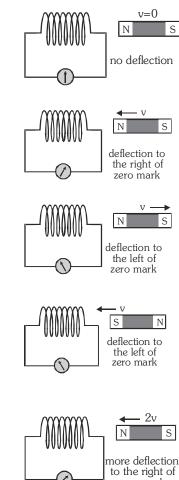
### 2. ELECTROMAGNETIC INDUCTION

Michael Faraday demonstrated the reverse effect of Oersted experiment. He explained the possibility of producing emf across the ends of a conductor when the magnetic flux linked with the conductor changes. This was termed as electromagnetic induction. The discovery of this phenomenon brought about a revolution in the field of electric power generation.

#### **FARADAY'S EXPERIMENT**

Faraday performed various experiments to discover and understand the phenomenon of electromagnetic induction. Some of them are :

- When the magnet is held stationary anywhere near or inside the coil,
   the galvanometer does not show any deflection.
- When the N-pole of a strong bar magnet is moved towards the coil,
   the galvanometer shows a deflection right to the zero mark.
- When the N-pole of a strong bar magnet is moved away from the coil,
   the galvanometer shows a deflection left to the zero mark.
- If the above experiments are repeated by bringing the S-pole of the, magnet towards or away from the coil, the direction of current in the coil is opposite to that obtained in the case of N-pole.
- The deflection in galvanometer is more when the magnet moves faster and less when the magnet moves slower.



### **CONCLUSIONS**

Whenever there is a relative motion between the source of magnetic field (magnet) and the coil, an emf is induced in the coil. When the magnet and coil move towards each other then the flux linked with the coil increases and emf is induced. When the magnet and coil move away from each other the magnetic flux linked with the coil decreases, again an emf is induced. This emf lasts so long as the flux is changing.

Due to this emf an electric current start to flow and the galvanometer shows deflection.

The deflection in galvanometer last as long the relative motion between the magnet and coil continues.

Whenever relative motion between coil and magnet takes place an induced emf produced in coil. If coil is in closed circuit then current and charge is also induced in the circuit. This phenomenon is called electro magnetic induction.



### 3. FARADAY'S LAWS OF ELECTROMAGNETIC INDUCTION

Based on his experimental studies on the phenomenon of electromagnetic induction, Faraday proposed the following two laws.

#### First law

Whenever magnetic flux linked with a closed circuit changes, an emf is induced in the circuit. The induced emf lasts so long as the change in magnetic flux continues.

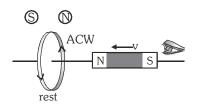
#### Second law

The magnitude of emf induced in a closed circuit is directly proportional to rate of change of magnetic flux linked with the circuit. If the change in magnetic flux in a time dt is d $\phi$  then  $e \propto \frac{d\phi}{dt}$ 

### 4. LENZ'S LAW

The Russian scientist H.F. Lenz in 1835 discovered a simple law giving the direction of the induced current produced in a circuit. Lenz's law states that the induced current produced in a circuit always flow in such a direction that it opposes the change or cause that produced it. If the coil has N number of turns and  $\phi$  is the magnetic flux linked with each turn of the coil then, the total magnetic flux linked with the coil at any time =  $N\phi$ 

$$\therefore \ e = -\frac{d}{dt}(N\phi) = -N\frac{d\phi}{dt} = -\frac{N(\phi_2 - \phi_1)}{t}$$



CW V S

(Coil face behaves as North pole to oppose the motion of magnet.)

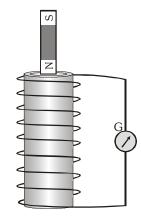
(Coil face behaves as South pole to oppose the motion of magnet.)

 $e = (-)\frac{d\phi}{dt}$ , here negative sign indicates the concept of Lenz law.

## LENZ'S LAW - A CONSEQUENCE OF CONSERVATION OF ENERGY

Copper coils are wound on a cylindrical cardboard and the two ends of the coil are connected to a sensitive galvanometer. When a bar magnet is moved towards the coil (fig.). The upper face of the coil near the magnet acquired north polarity.

Consequently work has to be done to move the magnet further against the force of repulsion. When we withdraw the magnet away from the coil, its nearer face acquires south polarity. Now the work done is against the force of attraction. When the magnet is moved, the number of magnetic lines of force linking the coil changes, which causes an induced current of flow through the coil. The direction of the induced current, according to Lenz's law is always to oppose the motion of the magent.

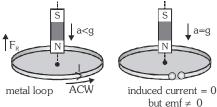


The work done in moving the magnet is converted into electrical energy. This energy is dissipated as heat energy in the coil. Therefore, the induced current always flows in such a direction to oppose the cause. Thus it is proved that Lenz's law is the consequence of conservation of energy.



### **GOLDEN KEY POINTS**

- Induced emf does not depends on nature of the coil and its resistance.
- Magnitude of induced emf is directly proportional to the relative speed of coil magnet system, (e  $\propto$  v).
- Induced current also depends on resistance of coil (or circuit).
- Induced emf does not depends on resistance of circuit, It exist in open circuit also.

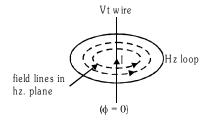


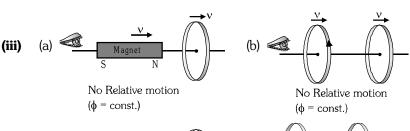
- In all E.M.I. phenomenon, induced emf is non-zero induced parameter.
- Induced charge in any coil (or circuit) does not depend on time in which change in flux occurs i.e. it is independent
  from rate of change of flux or relative speed of coil—magnet system.
- Induced charge depends on change in flux through the coil and nature of the coil (or circuit) i.e. resistance.

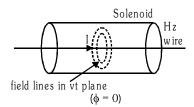
### • NO E.M.I. CASES

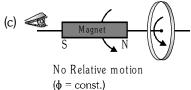
### Cases

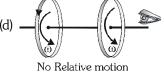
- (i) If current I increases with respect to time, no emf induced in loop because no flux associated with it, as plane of circular field lines of straight wire is parallel to the plane of loop.
- (ii) If current I increases with respect to time no emf induced in solenoid because no flux associated with solenoid



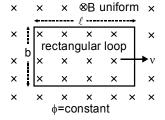




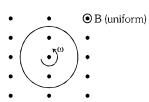




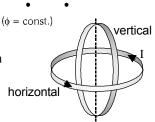
 $(\phi = \text{const.})$ 



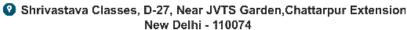
- (iv) Any rectangular coil or loop translates within the uniform transverse magnetic field, no emf induced in it because its flux remains constant.
- (v) Any coil or loop rotates about its geometrical axis in uniform transverse magnetic field, no emf induced in it because its flux remains constant.



(vi) If current of one coil (or loop) either increase or decrease, no emf induced in another coil (or loop) because no flux associated for the coils (or loops) which are placed mutually perpendicular.







# - Illustrations -

### Illustration 4.

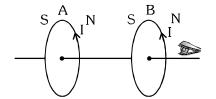
Two idential co-axial circular coils carries equal currents :-

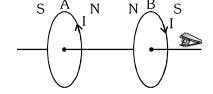
(a) In same direction

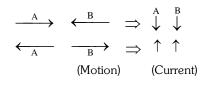
(b) In opposite direction.

If both the coils moves towards each other and away from each other respectively then current in both coils :-

- (1) Increases
- (2) Decreases
- (3) Remains same
- (4) None





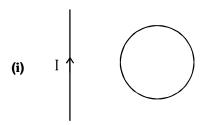


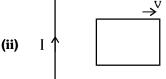
# **BEGINNER'S BOX-2**

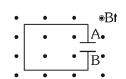
 $\boldsymbol{1.} \hspace{0.5cm} \text{Find direction of induced current for the given cases} :-$ 

(Where w.r.t. = with respect to time, ob = observer = (1)

(v)



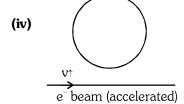




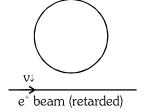
(iii)

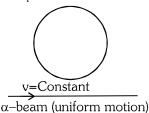
(vi)

What is the nature of charge on plates of capacitor?

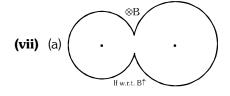


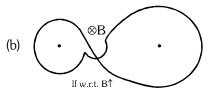
If I ↑ w.r.t.

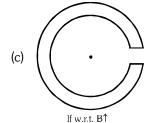


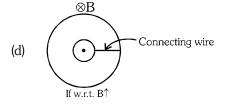


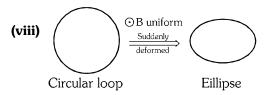
 $\otimes B$ 







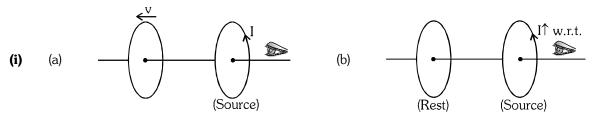




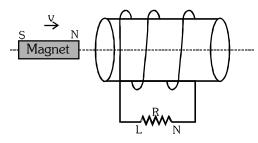


Shrivastava Classes, D-27, Near JVTS Garden, Chattarpur Extension New Delhi - 110074

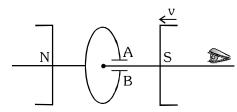
# **2.** Find direction of induced current in the given cases :-



(ii) What is the direction of induced current in resistance 'R'?



(iii) What is the nature of the charge on the plates of capacitor?



# 5. INDUCED PARAMETERS

- (i) Induced emf (e)
- (ii) Induced current (I)
- (iii) Induced charge (q)

- (iv) Induced heat (H)
- (v) Induced electric field  $(E_{_{\!\scriptscriptstyle in}})$

Let for a coil its mag. flux changes by  $\Delta \varphi$  in time interval  $\Delta t$  and total resistance of coil-circuit is R.

Now rate of change of flux 
$$=\frac{\Delta \phi}{\Delta t}$$
 Average induced emf  $e_{_{av}}=\frac{-\Delta \phi}{\Delta t}$ 

(i) Instantaneous induced emf 
$$e = \lim_{\Delta t \to 0} \left( \frac{-\Delta \phi}{\Delta t} \right)$$

$$e = -\frac{d\phi}{dt}$$

(ii) Induced current flow at this instant 
$$I = \frac{e}{R}$$

$$I = \frac{-1}{R} \left( \frac{d\phi}{dt} \right)$$

(iii) In time interval 
$$dt$$
, induced charge  $dq = Idt$ 

$$dq = -\frac{d\phi}{R}$$

(iv) Induced heat :- 
$$H = \int_{0}^{t} I^{2}Rdt = \int_{0}^{t} \frac{e^{2}}{R}dt$$



# (v) Induced electric field and its properties:

When magnetic field changes with time in region then an electric field induces within and outside the region.

- This field is different from the conservative electrostatic field produced by stationary charges.
- Its field lines are always in closed curves.
- Relation  $\vec{F} = q\vec{E}$  is valid for this field
- It is non-conservative in nature so concept of potential has no meaning in this field.
- For induced electric field  $\oint \vec{E}_{ind} \cdot d\vec{\ell} \neq 0$  (But for electrostatic field

$$\oint \vec{E} \cdot d\vec{\ell} = 0 \; ; \; always)$$

- When a unit charges goes once around the loop the total work on it by the electric field is equal to emf in loop.
- From faraday law of emf  $e = -\frac{d\phi}{dt}$  or  $\oint \vec{E}_{ind} \cdot d\vec{\ell} = -\frac{d\phi}{dt}$
- Direction of induced electric field is the same as direction of induced current.

$$E_{ind}$$
 due to  $\frac{dB}{dt}$  :-

Use 
$$\oint \vec{E}_{ind} \cdot d\vec{\ell} = -\frac{d\phi}{dt}$$
 and for

symmetrical situation 
$$E\ell=\left|\frac{d\varphi}{dt}\right|=\frac{AdB}{dt}$$

 $\ell$  = length of closed loop

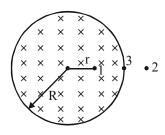
A = Area in which magnetic field is changing

### Case I (r < R) (inside):

$$E(2\pi r) = \frac{AdB}{dt}$$

$$E(2\pi r) = \pi r^2 \left(\frac{dB}{dt}\right)$$

$$E = \frac{r}{2} \frac{dB}{dt} \quad (E_{inside} \propto r)$$



Concentric circular field lines

of  $\vec{E}_{induce}$  (inside/outside)

# Case II (r > R) outside:

$$E(2\pi r) = A\left(\frac{dB}{dt}\right)$$

$$E(2\pi r) = \pi R^2 \left(\frac{dB}{dt}\right) \qquad \Rightarrow \qquad \boxed{E = \frac{R^2}{2r} \frac{dB}{dt}} \quad (E_{out} \propto \frac{1}{r})$$

### Case III (r = R) surface:

$$E(2\pi R) = \pi R^2 \left(\frac{dB}{dt}\right) \qquad \Rightarrow \qquad \boxed{E = \frac{R}{2} \frac{dB}{dt}}$$



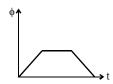
# **BEGINNER'S BOX-3**

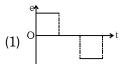
- 1. Flux linked through following coils changes with respect to time then for which coil an e.m.f. is not induced:-
  - (1) Copper coils
- (2) Wood coil
- (3) Iron coil
- (4) None
- 2. A coil and a magnet moves with their constant speeds 5 m/sec. and 3 m/sec. respectively, towards each other, then induced emf in coil is 16 mV. If both are moves in same direction, then induced emf in coil:-
  - (1) 15 mV
- (2) 4 mV
- (3) 64 mV
- (4) Zero
- 3. Magnetic flux  $\phi$  (in Weber) linked with a closed circuit of resistance 10 ohm varies with time t (in seconds) as  $\phi = 5t^2 4t + 1$ . The induced emf in the circuit at t = 0.2 sec. is :-
  - (1) 0.4 V
- (2) 0.4 V
- (3) 2.0 V
- (4) 2.0 V

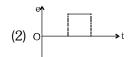
**4.** Magnetic flux linked through the coil changes

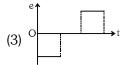
with respect to time according to following

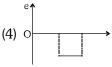
graph, then induced emf v/s time graph for coil is :-











- **5.** The radius of a circular coil having 50 turns is 2 cm. Its plane is normal to the magnetic field. The magnetic field changes from 2T to 4T in 3.14 sec. The induced emf in coil will be :-
  - (1) 0.4V
- (2) 0.04V
- (3) 4 mV
- (4) 0.12 V
- 6. Magnetic field changes at the rate of 0.4 T/sec. in a square coil of side 4 cm. kept perpendicular to the field. If the resistance of the coil is  $2 \times 10^{-3} \Omega$ , then induced current in coil is :-
  - (1) 0.16 A
- (2) 0.32 A
- (3) 3.2 A
- (4) 1.6 A
- **7.** A short bar magnet allowed to fall along the axis of horizontal metallic ring. Starting from rest, the distance fallen by the magnet in one second may be :-
  - (1) 4.0 m.
- (2) 5.0 m.
- (3) 6.0 m.
- (4) 7.0 m.
- **8.** In a circuit a coil of resistance  $2\Omega$ , then magnetic flux changes from 2.0Wb to 10.0Wb in 0.2 sec. The charge flow in the coil during this time is :-
  - (1) 5.0 C
- (2) 4.0 C
- (3) 1.0 C
- (4) 0.8 C
- **9.** A circular loop of radius 2cm, is placed in a time varing magnetic field with rate of 2T/sec. Then induced electric field in this loop will be :-
  - (1) 0

- (2) 0.02 V/m
- (3) .01 V/m
- (4) 2 V/m

### 6. TYPES OF E.M.I

For a loop flux, ( $\phi = BA \cos\theta$ ,) changes w.r.t. time in following three manner and according to it electro magnetic induction is classified in three ways :-

- (i) If  $(A, \theta) \rightarrow const$  &  $\frac{dB}{dt} \rightarrow \frac{d\phi}{dt}$   $\Rightarrow$  Static EMI (1) Self Induction (In this case EMI occurs for rest coil) (2) Mutual Induction
- (ii) If (B,  $\theta$ )  $\rightarrow$  const &  $\frac{dA}{dt}$   $\rightarrow \frac{d\phi}{dt}$   $\Rightarrow$  Dynamic EMI (In this case EMI occurs for a moving straight wire)
- (iii) If (A,B)  $\rightarrow$  const &  $\frac{d\theta}{dt}$   $\rightarrow$   $\frac{d\phi}{dt}$   $\Rightarrow$  **Periodic E.M.I** (In this case E.M.I. occurs for a rotating coil)



**STATIC E.M.I.** 
$$\Rightarrow \frac{dI}{dt} \rightarrow \frac{dB}{dt} \rightarrow \frac{d\phi}{dt} \Rightarrow \text{Static EMI}$$

### 7. SELF INDUCTION

When current through the coil changes, with respect to time then magnetic flux linked with the coil also changes with respect to time. Due to this an emf and a current induced in the coil. According to Lenz law induced current opposes the change in magnetic flux. This phenomenon is called self induction and a factor by virtue of which the coil shows opposition for change in magnetic flux called self inductance of coil. Considering this coil circuit in two cases:

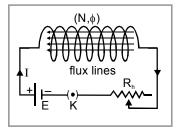
# Case-I: Current through the coil is constant:-

If 
$$I \rightarrow B \rightarrow \phi \rightarrow Const. \Rightarrow No EMI$$

total flux of coil (N $\phi$ )  $\infty$  current through the coil

 $N\phi \propto \, I$ 

 $N\phi = LI$ 



$$L = \frac{N\phi}{I} = \frac{NBA}{I} = \frac{\phi_{Total}}{I} \quad \text{,Where $L:$ self inductance of coil}$$

S.I. unit of L 
$$\rightarrow$$
 1  $\frac{\text{weber}}{A}$  =1 henry =  $1\frac{N-m}{A^2}$  =  $1\frac{J}{A^2}$  Dimensions : [M¹L²T⁻² A⁻²]

**Sp. Note :-** L is constant of coil it **does not depends on current** through the coil.

Case-II: Current through the coil changes w.r.t.:

If 
$$\frac{dI}{dt} \rightarrow \frac{dB}{dt} \rightarrow \frac{d\phi}{dt} \Rightarrow Static EMI$$

$$N\phi = LI$$

$$-\ N\ \frac{d\varphi}{dt}\ = -\ L\ \frac{dI}{dt}\,,\ \ \text{where}\ -\ N\ \frac{d\varphi}{dt}\ \ \text{called self induced emf of coil 'e_s'}$$

$$e_s = -L \frac{dI}{dt}$$
 S.I. unit of  $L \rightarrow \frac{V-sec}{A}$ 

#### Self-inductance of a solenoid

Let cross-sectional area of solenoid=A, Current flowing through it=I

$$\mbox{Length of the solenoid } = \ell, \mbox{ then } \phi = NBA = N \frac{\mu_0 N I}{\ell} A = \frac{\mu_0 N^2 A}{\ell} I$$

But 
$$\phi = LI$$
 :  $L = \frac{\mu_0 N^2 A}{\ell}$  or  $L_m = \frac{\mu_0 \mu_r N^2 A}{\ell}$ 

If no iron or similar material is nearby, then the value of self-inductance depends only on the geometrical factors (length, cross-sectional area, number of turns).



# Illustrations

#### Illustration 6.

The current in a solenoid of 240 turns, having a length of 12 cm and a radius of 2 cm, changes at the rate of  $0.8 \text{ As}^{-1}$ . Find the emf induced in it.

#### Solution

$$\mid \mathcal{E} \models L \frac{dI}{dt} = \frac{\mu_0 N^2 A}{\ell} \cdot \frac{dI}{dt} = \frac{4\pi \times 10^{-7} \times (240)^2 \times \pi \times (0.02)^2}{0.12} \times 0.8 = 6 \times 10^{-4} \, V$$

#### Illustration 7.

A soft iron core is introduced in an inductor. What is the effect on the self-inductance of the inductor?

### **Solution**

Since soft iron has a large relative permeability therefore the magnetic flux and consequently the self-inductance is considerably increased.

# **BEGINNER'S BOX-4**

1 The value of self inductance of a coil is 5H. The value of current changes from 1A to 2A in 5 sec., then value of induced emf in it:-

(1) 10V

(2) 0.1V

(3) 1.0V

(4) 100V

**2** A coil of self inductance 2H carries a 2A current. If direction of current is reversed in 1 sec., then induced emf in it:-

(1) - 8V

(2) 8V

(3) - 4V

(4) Zero

3 For a coil having L=2mH, current flow through it is  $I=t^2e^{-t}$  then the time at which emf becomes zero:-

(1) 2 sec.

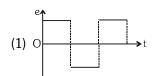
(2) 1 sec.

(3) 4 sec.

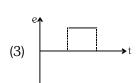
(4) 3 sec.

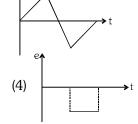
4 Current through the coil varies according to graph

then induced emf v/s time graph is



(2) O





**5.** A solenoid have the self inductance 2H. If length of the solenoid is doubled having turn density and area constant then new self inductance is :-

(1) 4F

(2) 1H

(3) 8H

(4) 0.5 H

**6.** A solenoid wound over a rectangular frame. If all the linear dimensions of the frame are increased by a factor 3 and the number of turns per unit length remains the same, the self inductance increased by a factor of :-

(1) 3

(2) 9

(3) 27

(4) 63

**7.** A coil of inductance 2 H has a current of 5.8 A. The flux in weber through the coil is :-

(1) 0.29

(2) 2.9

(3) 3.12

(4) 11.6

### 8. R-L D.C. CIRCUIT

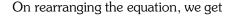
### Case I: Current Growth:

Consider an inductance L and a resistance R (including the resistance of the coil L) connected in series to a battery of emf E. When the switch S is closed, the current in the circuit begins to grow. After the key is closed the current changes from zero to some value. The current rises gradually rather than instantly. It takes some time before the current reaches its steady value  $I_0 = E/R$ . The effect of the inductance in a dc circuit is to increase the time taken by the current to reach its limiting value  $I_0$ .



At any instant, Kirchoff's voltage law for the loop gives

$$E - L \frac{dl}{dt} = RI$$

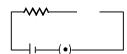


$$\frac{dl}{\frac{E}{R} - I} = \frac{R}{L}dt$$

On integrating both the sides we get

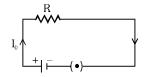
$$\boxed{I = I_0 (1 - e^{-t/\lambda})} \text{ where } I_0 = \frac{E}{R} \text{ and } \lambda = \frac{L}{R}$$

(i) Just after the closing of the key inductance behaves like open circuit and current in circuit is zero.



(Open circuit, t = 0, I = 0) (Inductor provide infinite resistence)

(ii) Some time after closing of the key inductance behaves like simple connecting wire (short circuit) and current in circuit is constant.



(Short circuit,  $t \to \infty$ ,  $I \to I_0$ ) (Inductor provide zero resistence)

(Final, steady, maximum or peak value of current)

Sp. Note: Peak value of current in circuit does not depends on self inductance of coil.

(iii) Time constant of circuit ( $\lambda$ ):  $\left|\lambda = \frac{L}{R}\right|$  Its SI unit is second(s)

It is a time in which current increases up to 63% or 0.63 times of peak current value.

(iv) Half life (T) - It is a time in which current increases upto 50% or 0.50 times of peak current value.  $I = I_0 (1 - e^{-t/\lambda})$ 

$$t = T, I = I_0/2$$

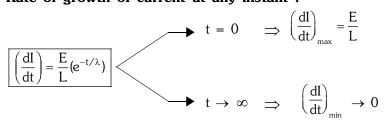
$$t \, = \, T, \, \, I \, = \, I_{_{\! 0}}/2\} \hspace{1cm} \frac{I_{_{\! 0}}}{2} \, \, = \, I_{_{\! 0}} \, \, (1 \, - \, e^{-T/\lambda}) \Rightarrow \, \, e^{-T/\lambda} \, = \, \frac{1}{2} \, \, \Rightarrow e^{T/\lambda} \, = \, 2$$

$$\frac{T}{\lambda}\log_e e = \log_e 2$$

$$T = 0.693\lambda$$

$$T = 0.693 \frac{L}{R} \text{ sec}$$

(v) Rate of growth of current at any instant :-



Sp. Note: Maximum or initial value of rate of growth of current does not depends upon resistance of coil.

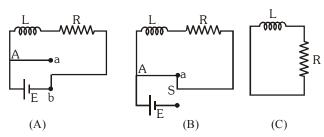


000000

Switch

### Case-II: Current Decay:-

Consider the arrangement shown in figure (A). The sliding switch S can be slided up and down. Let the switch S connect the point b. The circuit is complete and a steady current  $i = I_0$  is maintained through the circuit. Suddenly at t = 0, the switch S is moved to connect the point a. This completes the circuit through the wire Aa and disconnects the battery from the circuit [Figure (B)]. The special arrangement of the switch ensures that the circuit through the wire Aa is completed before the battery is is disconnected. (Such a switch is called make before break switch). The equivalent circuit is redrawn in figure (C).



As the battery is disconnected, the current decreased in the circuit. This induced as emf is the inductor. As this is only emf in the circuit, we have

$$-L\frac{dl}{dt} = RI$$
 or  $\frac{dl}{I} = -\frac{R}{L}dt$ 

on integrating both the sides, we get

$$I = I_0 e^{\frac{-Rt}{L}} = I_0 e^{-t/\lambda}$$

where  $\lambda = L/R$  is the time constant of the circuit.

(Just after opening of key)  $t = 0 \Rightarrow I = I_0 = \frac{E}{R}$ 

(Some time after opening of key)  $t \rightarrow \infty \Rightarrow I \rightarrow 0$ 

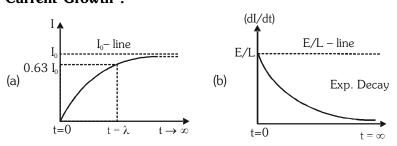
- (i) Time constant ( $\lambda$ ): It is a time in which current decreases up to 37% or 0.37 times of peak current value  $\lambda = \frac{L}{sec}$
- (ii) Half life (T) :- It is a time in which current decreases upto 50% or 0.50 times of peak current value.  $T = (0.693)\lambda \sec$
- (iii) Rate of decay of current at any instant :-

$$t = 0 \Rightarrow \left(-\frac{dI}{dt}\right)_{max.} = \frac{E}{L}$$

$$t \to \infty \Rightarrow \left(-\frac{dI}{dt}\right)_{min} \to 0$$

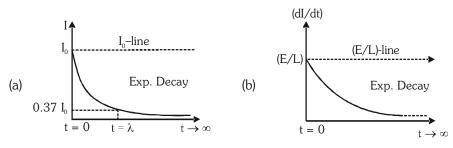
Special graph for R-L circuit :-

• Current Growth :-





## • Current decay :-



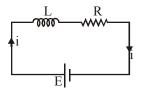
### 9. ENERGY STORED IN AN INDUCTOR

The battery that estabilishes the current in an inductor has to do work against the opposing induced emf. The energy supplied by the battery is stored in the inductor.

Let i be the instantaneous current in the LR circuit. Applying Kirchoff's voltage law, we get

$$E = iR + L\frac{di}{dt}$$

The instantaneous power supplied by the battery is given by



$$P = Ei = i^2R + Li\frac{di}{dt}$$

where  $i^2R$  is the power dissipated in the resistor and the last term represent the rate average energy U is being supplied to the inductor. That is,

$$\frac{dU}{dt} = Li \frac{di}{dt}$$
 or  $dU = Li di$ 

The total energy stored when the current increases from 0 to I is found by integration,

$$U = L \int_{0}^{I} i di = \frac{1}{2} L I^{2} \implies \boxed{U = \frac{1}{2} L I^{2}}$$

### **Energy Density of Inductor**

For a solenoid the inductance is given as

$$L = \mu_0 n^2 lA$$

Since B = 
$$\mu_0 n I$$
, therefore, L =  $\frac{B^2 A \ell}{\mu_0 I^2}$ 

Thus, the energy stored in the solenoid is

$$U = \frac{1}{2}LI^2 = \frac{B^2}{2\mu_0}(A\ell)$$

Since  $A\ell$  is the volume of the solenoid therefore energy stored per unit volume =  $\left| \frac{U}{A\ell} = \frac{B^2}{2\mu_0} \right|$ 

Although we derived this result for a special case i.e. the solenoid but it is true in general.

Thus the energy density of a magnetic field in free space =  $\frac{B^2}{2\mu_0}\,.$ 



# **GOLDEN KEY POINTS**

• Thin wire  $R \neq 0 \& L = 0 \Rightarrow R$  Role of  $R \rightarrow$  to opposes flow of current, now this wire moulded in form of coil.

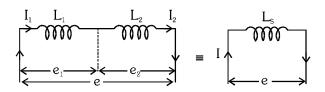
becomes constant, then no role of 'L'

Sp. Note: Resistance is possible without inductance but inductance is not possible without resistance.

- If w.r.t. I  $\uparrow \Rightarrow \frac{dI}{dt}$  (+ve)  $\Rightarrow e_s$  (-ve) opposite emf  $\Rightarrow E_{net} = E e_s$
- $\bullet \qquad \text{If w.r.t. I} \; \downarrow \; \Rightarrow \quad \frac{dI}{dt} \text{(-ve)} \; \Rightarrow \; e_{_{s}} \; \text{(+ve) same directed emf} \; \Rightarrow \; \boxed{E_{\text{net}} = E + e_{_{s}}}$
- Current variation with key :-
  - (a) Just closing of key  $\Rightarrow$  I  $\uparrow$  = dI (+ve)  $\Rightarrow$  e (-ve)
  - (b) Just opening of key (source emf E cut out)  $\Rightarrow$  I  $\downarrow$  = dI (-ve)  $\Rightarrow$  e<sub>s</sub> (+ve)
  - (c) At the time of sudden opening of key, due to high inductance of circuit a high momentarily emf (surge) induces and sparking occurs at key position. To avoid sparking a capacitor is connected parallel to the key.
- Self inductance always opposes the change of current in electric circuit so it is also called inertia of electric circuit.

# Combination of Inductances:

### (a) Series fashion:



Potential devides,  $e = e_1 + e_2$ 

$$L_s \frac{dI}{dt} = L_1 \frac{dI_1}{dt} + L_2 \frac{dI_2}{dt}$$
 (as  $e = -L \frac{dI}{dt}$ )

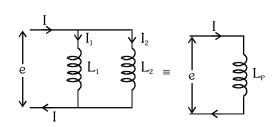
Current remains same  $I = I_1 = I_2$  i.e.  $\frac{dI}{dt} = \frac{dI_1}{dt} = \frac{dI_2}{dt}$ ;  $L_S = L_1 + L_2$ 

### (b) Parallel fashion:

Current devides, 
$$I = I_1 + I_2$$

$$\frac{\mathrm{dI}}{\mathrm{dt}} = \frac{\mathrm{dI}_1}{\mathrm{dt}} + \frac{\mathrm{dI}_2}{\mathrm{dt}}$$

$$\frac{e}{L_P} = \frac{e_1}{L_1} + \frac{e_2}{L_2} \left[ \text{as } e = -L \frac{dI}{dt} \text{ i.e. } \frac{dI}{dt} = -\frac{e}{L} \right]$$



Potential remains same,  $e = e_1 = e_2$ 

$$\frac{1}{L_{P}} = \frac{1}{L_{1}} + \frac{1}{L_{2}} \Rightarrow \boxed{L_{P} = \frac{L_{1}L_{2}}{L_{1} + L_{2}}}$$



# Illustrations

### Illustration 8.

An electromagnet has stored  $648 \, \mathrm{J}$  of magnetic energy, when a current of 9A exists in its coils. What average emf is induced if the current is reduced to zero in  $0.45 \, \mathrm{s}$ ?

### **Solution:**

Magnetic energy 
$$U = \frac{1}{2}LI^2 \Rightarrow L = \frac{2U}{I^2} = \frac{2 \times 648}{9 \times 9} = 16H$$

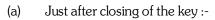
Induced emf 
$$e = L\left(\frac{\Delta I}{\Delta t}\right) = (16)\left(\frac{9}{0.45}\right) = 320V$$

### Illustration 9.

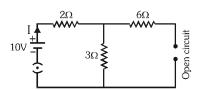
Calculate current, which given by battery for the following circuit.

- (a) Just after closing of the key.
- (b) Some time after closing of the key



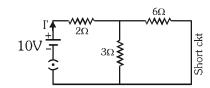


Current 
$$I = \frac{E}{r_{net}} = \frac{10}{2+3} = 2A$$



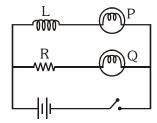
(b) Some time after Closing of the key:-

Current I' = 
$$\frac{E}{r_{net}} = \frac{10}{4} = 2.5A$$
, Where  $r_{net} = 2 + \frac{3 \times 6}{3 + 6}$ 



### Illustration 10.

Figure shows an inductor L, a resistor R connected in paralled to a battery through a switch. The resistance of resistor R is same as that of the coil that makes  $\ L$ . Two identical bulb are put in each arm of the circuit.



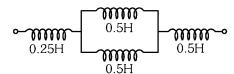
- (a) Which of two bulbs lights up earlier when S is closed?
- (b) Will the bulbs be equally bright after some time?

### **Solution:**

- (i) When switch is closed induced e.m.f. in inductor i.e. back e.m.f. delays the glowing of bulb P so bulb Q light up earlier.
- (ii) Yes. At steady state inductive effect becomes meaningless so both identical bulbs become equally bright after some time.

### Illustration 11.

Three inductances are connected as shown in figure. Find the equivalent inductance of circuit.



### **Solution:**

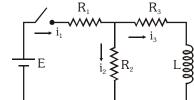
$$L_{\text{equivalent}} = 0.25 + \left(\frac{0.5 \times 0.5}{0.5 + 0.5}\right) + 0.5 = 1H$$



# **BEGINNER'S BOX-5**

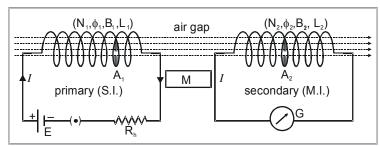
- **1.** L, C and R respectively indicate inductance, capacitance and resistance. Select the combination, which does not have dimensions of frequency:-
  - (1) 1/RC
- (2) R/L
- (3)  $1/\sqrt{LC}$
- (4) C/L
- **2.** A coil of 10 H inductance and  $5\Omega$  resistance is connected to 5 volt battery in series. The current in ampere in circuit 2 seconds after switched is on :-
  - (1) e

- (2)  $(1-e^{-1})$
- (3) (1-e)
- (4) e
- 3. An L-R circuit consists of an inductance of 8mH and a resistance of  $4\Omega$ . The time constant of the circuit is:-
  - (1) 2ms
- (2) 12ms
- (3) 32ms
- (4) 500 s
- **4.** In an L -R circuit, time constant is that time in which current grows from zero to the value (Where  $I_{\circ}$  is the steady state current) :-
  - $(1) 0.63 I_{0}$
- (2) 0.50 I
- (3) 0.371
- (4) I
- 5. An inductor of 20 H and a resistance of 10  $\Omega$ , are connected to a battery of 5 volt in series, then initial rate of change of current is :-
  - (1) 0.5 amp/s
- (2) 2.0 amp/s
- (3) 2.5 amp/s
- (4) 0.25 amp/s
- **6.** A coil of L= $5x10^{-3}$  H and R= $18~\Omega$  is abruptly supplied a potential of 5 volts. What will be the rate of change of current in 0.001 second ? ( $e^{-3.6} = 0.0273$ )
  - (1) 27.3 amp/sec.
- (2) 27.8 amp/sec.
- (3) 2.73 amp/sec.
- (4) 2.78 amp/sec.
- 7. A coil of inductance 8.4 mH and resistance  $6\Omega$  is connected to a 12V battery in series. The current in the coil is 1.0A at approximately the time :-
  - (1) 500s
- (2) 20s
- (3) 35ms
- (4) 1ms
- **8.** The dimensions of combination  $\frac{L}{CVR}$  are same as dimensions of :-
  - (1) Change
- (2) Current
- (3) Charge<sup>-1</sup>
- (4) Current<sup>-1</sup>
- 9. In the circuit shown in adjoining fig E = 10V,  $R_1 = 1\Omega$   $R_2 = 2\Omega$ ,  $R_3 = 3\Omega$  and L = 2H. Calculate the value of current  $i_1$ ,  $i_2$  and  $i_3$  immidiately after key S is closed:
  - (1) 3.3 amp, 3.3 amp, 3.3 amp
  - (2) 3.3 amp, 3.3 amp, 0 amp
  - (3) 3.3 amp, 0 amp, 0 amp
  - (4) 3.3 amp, 3.3 amp 1.1 amp



### 10. MUTUAL INDUCTION:

**Basic Concept:** Whenever current passing through primary coil or circuit change with respect to time then magnetic flux in neighbouring secondary coil or circuit will also changes with respect to time. According to Lenz Law for opposition of flux change an emf and a current induced in the neighbouring coil or circuit. This phenomenon called as 'Mutual induction'.



Due to Air gap,  $\phi_2 < \phi_1$  always and  $\phi_2 = B_1 A_2$  ( $\theta = 0^0$ ).



# Case-I: When current through primary is constant:-

Total flux of secondary is directly proportional to current flow through the primary coil

$$N_2 \phi_2 \propto I_1$$

$$N_2 \phi_2 = MI_1$$

$$M = \frac{N_2 \phi_2}{I_1} = \frac{N_2 B_1 A_2}{I_1} = \frac{\left(\phi_T\right)_s}{I_p} \quad , \ \, \text{Where} \ \, M \, : \, \text{mutual inductance of circuits.}$$

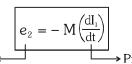
- The units and dimension of M are same as 'L'.
- The mutual inductance does not depends upon current through the primary and it is constant for both circuits.

# Case-II: When current through primary changes w.r.t.:

$$\text{If} \ \ \frac{dI_1}{dt} \, \to \frac{dB_1}{dt} \, \to \frac{d\varphi_1}{dt} \, \to \, \frac{d\varphi_2}{dt} \, \Rightarrow \, \text{Static EMI}$$

$$N_2 \phi_2 = MI_1$$

 $-N_2 \ \frac{d\varphi_2}{dt} = -M \frac{dI_1}{dt} \ , \ \left(-N_2 \frac{d\varphi_2}{dt}\right) \ \text{called total mutual induced emf of secondary coil} \ e_2.$ 

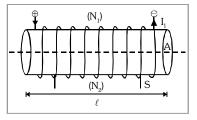


Secondary -

Different mutual inductances :-

- (a) In terms of their number of turns (b) In terms of their self inductances
- (a) In terms of their number of turns  $(N_1, N_2)$ :
- (1)Two co-axial solenoids  $(M_{S_1S_2})$ :-

$$\mathbf{M}_{\mathbf{s}_1\mathbf{s}_2} = \frac{\mathbf{N}_2\mathbf{B}_1\mathbf{A}}{\mathbf{I}_1}$$



$$= \ \frac{N_2}{I_1} \left( \frac{\mu_0 N_1 I_1}{\ell} \right) A, \ \text{where} \ B_1 = \ \frac{\mu_0 N_1 I_1}{\ell} \quad \Rightarrow \boxed{ M_{s_1 s_2} = \left( \frac{\mu_0 N_1 N_2 A}{\ell} \right) }$$

# (2)Two concentric and coplanar coils $(M_{C_1C_2})$ :-

$$M_{_{c_1c_2}} \ = \ \frac{N_2B_1A_2}{I_1} \quad , \ where \ B_1 \ = \ \frac{\mu_0N_1I_1}{2r_1} \ \& \quad A_2 \ = \ \pi{r_2}^2$$



# (b)In terms of their self inductances (L1,L2):

For two magnetically coupled coils :-

 $M = K\sqrt{L_1L_2}$ , where 'K' is coupling factor between two coils and its range  $0 \le K \le 1$ 

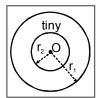
- For ideal coupling  $K_{max} = 1 \Rightarrow M_{max} = \sqrt{L_1 L_2}$  (Where M is geometrical mean of  $L_1 \& L_2$ )
- For real coupling (0 < K < 1)  $\Rightarrow$   $M = K\sqrt{L_1L_2}$
- Value of coupling factor 'K' decides from fashion of coupling.



# **GOLDEN KEY POINTS**

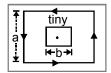
• Two concentric and coplanar loops :-

$$\boxed{ M \propto \frac{r_2^2}{r_1} } \quad (r_1 >> r_2)$$



• Two concentric and coplanar square loops :-

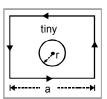
$$M \propto \frac{b^2}{a}$$

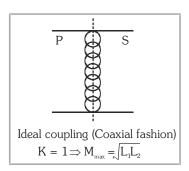


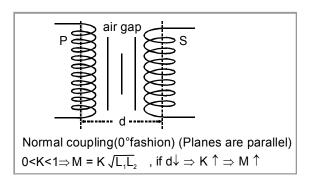
• A square and a circular concentric and coplanar loop :-

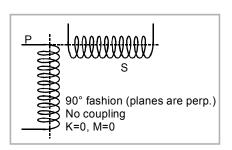
$$M \propto \frac{r^2}{a}$$

Different fashions of coupling :-









• 'K' also defined as  $k=\frac{\phi_s}{\phi_p}=\frac{mag. \ flux \ linked \ with \ Secondary}{mag. \ flux \ linked \ with \ Primary}$ 

# 'M' depends on :-

Number of turns (N<sub>1</sub>, N<sub>2</sub>)

Self inductances  $(L_1, L_2)$ 

Area of cross section

Magnetic permeabibility of medium (µ)

Distance between two coils (As  $d \downarrow = M \uparrow$ )

Orientation between two coils

Coupling factor 'K' between two coils.



# Illustrations -

### Illustration 12.

A solenoid has 2000 turns wound over a length of 0.3 m. The area of cross-section is  $1.2 \times 10^{-3}$  m<sup>2</sup>. Around its central section a coil of 300 turns is closely wound. If an initial current of 2A is reversed in 0.25 s, find the emf induced in the coil.

#### **Solution:**

$$M = \frac{\mu_0 N_1 N_2 A}{\ell} = \frac{4\pi \times 10^{-7} \times 2000 \times 300 \times 1.2 \times 10^{-3}}{0.3} = 3 \times 10^{-3} H$$

$$\mathcal{E} = -M \frac{\Delta I}{\Delta t} = -3 \times 10^{-3} \left[ \frac{-2 - 2}{0.25} \right] = 48 \times 10^{-3} V = 48 \text{ mV}$$

#### Illustration 13.

On a cylindrical rod two coils are wound one above the other. What is the coefficient of mutual induction if the inductance of each coil is  $0.1\,\mathrm{H}$ ?

### **Solution:**

One coil is wound over the other and coupling is tight, so K = 1,

$$M = \sqrt{L_1 L_2} = \sqrt{0.1 \times 0.1} = 0.1H$$

### Illustration 14.

How does the mutual inductance of a pair of coils change when:

- (i) the distance between the coils is increased?
- (ii) the number of turns in each coil is decreased?
- (iii) a thin iron rod is placed between the two coils, other factors remaining the same ? Justify your answer in each case .

### **Solution**

- (i) The mutual inductance of two coils, decreases when the distance between them is increased. This is because the flux passing from one coil to another decreases.
- (ii) Mutual inductance  $M = \frac{\mu_0 \; N_1 \; N_2 \; A}{\ell}$  i.e.,  $M \propto N_1 \; N_2$

Clearly, when the number of turns  $N_1$  and  $N_2$  in the two coils is decreased, the mutual inductance decreases.

(iii) When an iron rod is placed between th two coils the mutual inductance increases, because  $M \propto \text{permeability} (\mu)$ 

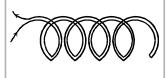
### Illustration 15.

A coil is wound on an iron core and looped back on itself so that the core has two sets of closely would wires in series carrying current in the opposite sense. What do you expect about its self-inductance? Will it be larger or small?

### **Solution:**

As the two sets of wire cartry currents in opposite directions, their induced emf's also act in opposite directions. These induced emf's tend to cancel each other, making the self-inductance of the coil very small.

**Note :** Resistance coil of resistance box, wound in two layer in opposite manner. the self inductance of coil becomes negligible



R ≠ 0

 $L \approx 0$  (Non inductive resistance)



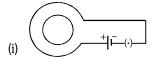
# **BEGINNER'S BOX-6**

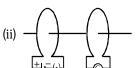
- 1. The mutual inductance between a primary and secondary circuits is 0.5H. The resistance of the primary and the secondary circuits are  $20\,\Omega$  and  $5\,\Omega$  respectively. To generate a current of  $0.4\,\mathrm{A}$  in the secondary, current in the primary must be changed at the rate of :-
  - (1) 4.0 A/s
- (2) 16.0 A/s
- (3) 16 A/s
- (4) 8 0 A/s
- 2. Two coils A and B having turns 300 and 600 respectively are placed near each other, on passing a current of 3.0 ampere in A, the flux linked with A is  $1.2 \times 10^{-4}$  weber and with B it is  $9.0 \times 10^{-5}$  weber. The mutual inductance of the system is :-
  - (1)  $2 \times 10^{-5}$  H
- (2)  $3 \times 10^{-5}$  H
- (3)  $4 \times 10^{-5} \text{ H}$
- (4)  $6 \times 10^{-5}$  H
- 3. If the current in a primary circuit is  $I=I_0$  Sin  $\omega t$  and the mutual inductance is M, then the value of induced voltage in secondary circuit will be :-
  - (1)  $e=MI \omega \cos \omega t$

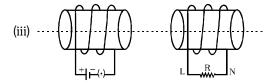
- (2)  $e=-MI_0\omega$  Cos  $\omega t$  (3)  $e=[M\omega$  Cos  $\omega t]/I_\omega$  (4)  $e=-(M\omega$  Cos  $\omega t)/I_\omega$
- 4. An a.c. of 50 Hz and 1 A peak value flows in primary coil transformer whose mutual inductance is 1.5 H. Then peak value of induced emf in secondary is :-
  - (1) 150 V
- (2)  $150 \pi V$
- (3) 300 V
- (4) 200 V
- 5. The number of turn of primary and secondary coil of a transformer is 5 and 10 respectively and the mutual inductance is 25 H. If the number of turns of the primary and secondary is made 10 and 5, then the mutual inductance of the coils will be :-
  - (1) 6.25 H
- (2) 12.5 H
- (3) 25 H
- (4) 50 H
- 6. The length of a solenoid is 0.3 m and the number of turns is 2000. The area of cross-section of the solenoid is  $1.2 \times 10^{-3}$  m<sup>2</sup>. Another coil of 300 turns is wrapped over the solonoid. A current of 2A is passed through the solenoid and its direction is changed in 0.25 sec. then the induced emf in coil :-
  - (1)  $4.8 \times 10^{-2} \text{ V}$
- (2)  $4.8 \times 10^{-3} \text{ V}$
- (3)  $3.2 \times 10^{-4} \text{ V}$
- (4)  $3.2 \times 10^{-2} \text{ V}$
- **7**. Two conducting loops of radi  $R_1$  and  $R_2$  are concentric and are placed in the same plane. If  $R_1 > R_2$ , the mutual inductance M between them will be directly proportional to :-
  - (1)  $R_1/R_2$
- (2)  $R_0/R_1$
- (3)  $R_1^2/R_2^2$
- (4)  $R_0^2/R_1$
- 8. Find direction of induced current in secondary circuit for the following changes in primary circuit :-
  - (a) Key is just closed

(b) Some time after the closing of key

(c) Key is just opened









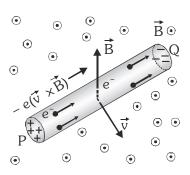
9810934436, 8076575278, 8700391727

# 11. **DYNAMIC E.M.I.** $\left[\frac{dA}{dt} \rightarrow \frac{d\phi}{dt}\right]$

free electrons is,  $\vec{F}_e = -e\vec{E}$ 

### Motional emf from Lorentz force

A conductor PQ is placed in a uniform magnetic field B, directed normal to the plane of paper outwards. PQ is moved with a velocity v, the free electrons of PQ also move with the same velocity. The electrons experience a magnetic Lorentz force,  $F_{m}=-e(\vec{v}\times\vec{B})$ . According to Fleming's left hand rule, this force acts in the direction PQ and hence the free electrons will move towards Q. A negative chagre accumulates at Q and a positive charge at P. An electric field E is setup in the conductor from P to Q. Force exerted by electric field on the



The accumulation of charge at the two ends continues till these two forces balance each other.

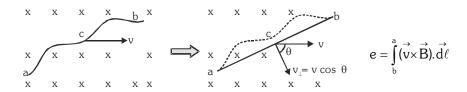
so 
$$\vec{F}_m = -\vec{F}_e \Rightarrow e(\vec{v} \times \vec{B}) = -e\vec{E} \Rightarrow \vec{E} = -(\vec{v} \times \vec{B})$$

The potential difference between the ends P and Q is  $V=-\vec{E}.\vec{\ell}=(\vec{v}\times\vec{B}).\vec{\ell}$ . It is the magnetic force on the moving free electrons that maintains the potential difference and produces the emf  $\mathcal{E}=B\;\ell\;v$  (for  $\vec{B}\perp\vec{v}\perp\vec{\ell}$ )

As this emf is produced due to the motion of a conductor, so it is called a motional emf.

The concept of motional emf for a conductor can be generalized for any shape moving in any magnetic field uniform or not. For an element  $\vec{d\ell}$  of conductor the contribution de to the emf is the magnitude  $d\ell$  multiplied by the component of  $\vec{v} \times \vec{B}$  parallel to  $\vec{d\ell}$ , that is  $de = (\vec{v} \times \vec{B}) \cdot \vec{d\ell}$ 

For any two points a and b the motional emf in the direction from b to a is,



Motional emf in wire acb in a uniform magnetic field is the motional emf in an imaginary wire ab. Thus,  $e_{acb} = e_{ab} = (length of ab) (v_{\perp}) (B)$ ,  $v_{\perp} = the component of velocity perpendicular to both <math>\overrightarrow{B}$  and ab. From right hand rule: b is at higher potential and a at lower potential. Hence,  $V_{ba} = V_b - V_a = (ab) (v \cos\theta)$  (B)

# ullet Direction of induced current or HP end of the rod find out with the help (HP $\rightarrow$ Higher potential) of

# (i) Fleming right hand rule

Fore finger  $\rightarrow$  In external field  $\vec{B}$  direction.

Thumb  $\rightarrow$  In the direction of motion ( $\vec{v}$ ) of conductor.

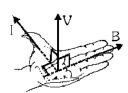
Middle finger → It indicates HP end of conductor/direction of induced current.

# (ii) Left hand palm rule

Fingers  $\rightarrow$  In external field ( $\vec{B}$ ) direction.

Palm  $\rightarrow$  In direction of motion  $(\vec{v})$  of conductor.

Thumb → It indicates HP end of conductor/direction of induced current in conductor.

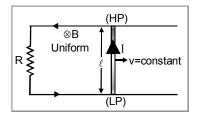




9810934436, 8076575278, 8700391727

# Motion of straight conductor in horizontal plane

For the given circuit, If metal rod moves with uniform velocity 'v' by an external agent.



- Induced emf in circuit  $| e = Bv \ell |$
- $I = \frac{e}{R} = \frac{Bv\ell}{R}$ Current flows through circuit
- Retarding opposing force exerted on metal rod by action of induced current

$$\vec{F}_{_{m}} = I(\vec{\ell} \times \vec{B}\,) \quad \Rightarrow F_{_{m}} = BI\ell, \quad \text{where} \quad \theta = 90^{o} \qquad \boxed{F_{_{m}} = \frac{B^{2}\ell^{2}v}{R}}$$

External mechanical force required for uniform velocity of metal rod.

For constant velocity resultant force on metal rod must zero and for that  $F_{ext} = F_{m}$ 

$$\boxed{F_{\text{ext.}} = F_{\text{m}} = \frac{B^2 \ell^2 v}{R}} \quad \Rightarrow \text{If (B, } \ell, \ R) \to \text{const.} \ \Rightarrow \boxed{F_{\text{ext.}} \propto v}$$

For uniform motion of metal rod, The rate of doing mechanical work by extenal agent or mechanical power delivered by external source given as :-

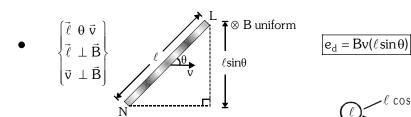
$$P_{\text{mech}} = p_{\text{ext}} = \vec{F}_{\text{ext}} \cdot \vec{v} = F_{\text{ext}} v$$

$$\boxed{ p_{\text{ext.}} = p_{\text{m}} = \frac{B^2 \ell^2 v^2}{R} } \quad \Rightarrow \text{If (B.$\ell$,R)} \ \to \text{const.} \ \Rightarrow \boxed{ p_{\text{mech.}} \propto v^2 }$$

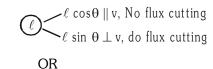
Rate of heat dissipation across resistance or thermal power developed across resistance is :-

$$P_{\text{th}} = \, I^2 R \, = \, \frac{1}{R} \left( \frac{B \nu \ell}{R} \right)^2 \quad \Rightarrow \left[ p_{\text{th}} = \frac{B^2 \ell^2 v^2}{R} \right] \label{eq:pth}$$

It is clear that  $p_{th} = p_{mech}$  which is consistent with the principle of conservation of energy.

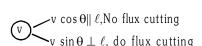


$$e_{d} = Bv(\ell \sin \theta)$$





$$e_{\rm d} = B(v \sin \theta)\ell$$





# Illustrations

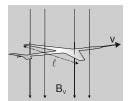
#### Illustration 16.

An aircraft with a wing span of 40 m flies with a speed of  $1080 \, \text{kmh}^{-1}$  in the eastward direction at a constant altitude in the northern hemisphere, where the vertical component of earth's magnetic field is  $1.75 \times 10^{-5} \, \text{T}$ . Find the emf that develops between the tips of the wings.

### **Solution**

The metallic part between the wing-tips can be treated as a single conductor cutting flux-lines due to vertical component of earth's magnetic field. So emf is induced between the tips of its wings.

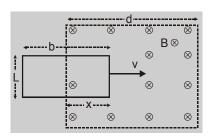
$$\begin{aligned} \text{HereI} &= 40 \text{ m}, \ B_v = 1.75 \times 10^{-5} \, \text{T} \\ v &= 1080 \, \text{kmh}^{-1} = \frac{1080 \times 1000}{3600} \text{ms}^{-1} = 300 \, \text{ms}^{-1} \\ \therefore \quad \mathcal{E} &= B_v \, \ell \, \, \text{v} = 1.75 \times 10^{-5} \times 40 \times 300 = 0.21 \, \text{V} \end{aligned}$$



### Illustration 17.

Figure shows a rectangular conducting loop of resistance R, width L, and length b being pulled at constant speed v through a region of width d in which a uniform magnetic field B is set up by an electromagnet.Let L=40 mm, b=10 cm, d=15 cm,  $R=1.6\ \Omega,\,B=2.0\ T$  and v=1.0 m/s

- (i) Plot the flux  $\phi$  through the loop as a function of the position x of the right side of the loop.
- (ii) Plot the induced emf as a function of the position of the loop.



#### Solution

(i) When the loop is not in the field:

The flux linked with the loop  $\phi = 0$ 

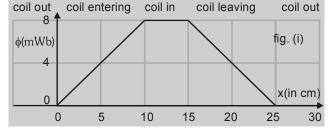
When the loop is entirely in the field:

Magnitic flux linked with the loop

$$\phi = BLb = 2 \times 40 \times 10^{-3} \times 10 \times 10^{-2} = 8 \text{ m Wb}$$

When the loop is entering the field:

The flux linked with the loop  $\phi = B L x$ 



When the loop is leaving the field:

The flux 
$$\phi = B L [b - (x - d)]$$

(ii) Induced emf is 
$$e = -\frac{d\phi}{dt} = -\frac{d\phi}{dx}\frac{dx}{dt} = -\frac{d\phi}{dx}v = -$$
 slope of the curve of figure (i)  $\times v$ 

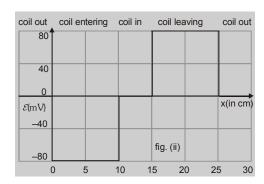
The emf for 0 to 10 cm:

$$e = -\frac{(8-0) \times 10^{-3}}{(10-0) \times 10^{-2}} \times 1 = -80 \,\text{mV}$$

The emf for 10 to 15 cm :  $e = 0 \times 1 = 0$ 

The emf for 15 to 25 cm:

$$e = -\frac{(0-8)\times10^{-3}}{(25-15)\times10^{-2}}\times1 = +80\,\text{mV}$$



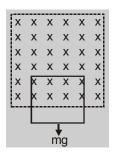


#### Illustration 18.

A horizontal magnetic field B is produced across a narrow gap between square iron pole-pieces as shown. A closed square wire loop of side  $\ell$ , mass m and resistance R is allowed of fall with the top of the loop in the field. Show that

the loop attains a terminal velocity given by  $v=\frac{Rmg}{B^2\ell^2}$  while it is between the

poles of the magnet.



### **Solution:**

As the loop falls under gravity, the flux passing through it decreases and so an induced emf is set up in it. Then a force F which opposes its fall. When this force becomes equal to the gravity force mg, the loop attains a terminal velocity v.

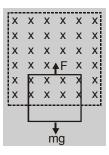
The induced emf  $e = B v \ell$ , and the induced current is  $i = \frac{e}{R} = \frac{Bv \ell}{R}$ 

The force experienced by the loop due to this current is  $\,F=B\,\,\ell\,i=\frac{B^2\,\nu\,\ell^2}{R}$ 

When v is the terminal (constant) velocity F = mg

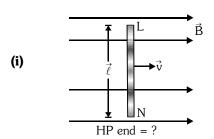
or 
$$\frac{B^2 v \ell^2}{R} = m_0$$

or 
$$v = \frac{Rmg}{B^2 \ell^2}$$

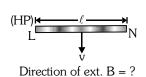


# **BEGINNER'S BOX-7**

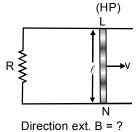
1. Find the Given Parameter when straight conductor moves in external magnetic field :-



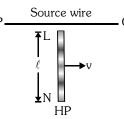
(ii)



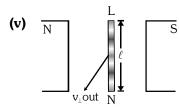
(iii)



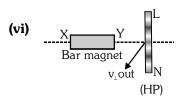
(iv)



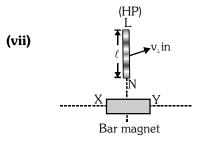
Direction of current in source wire PQ = ?



LP end = ?



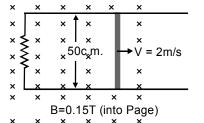
Poles of magnet=?



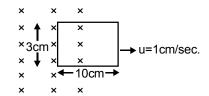
Poles of magnet = ?



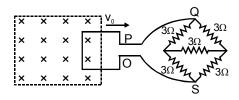
2. A metallic rod completes its circuit as shown in the figure. The circuit is normal to a magnetic field of B = 0.15 T. If the resistance of the circuit is  $3\Omega$  the force required to move the rod with a constant velocity of 2m/sec. is:



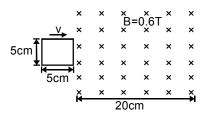
- (1) 3.75 x 10<sup>-3</sup> N
- (2)  $3.75 \times 10^{-2} \text{ N}$
- (3) 3.75 x 10<sup>2</sup> N
- (4)  $3.75 \times 10^{-4} \text{ N}$
- 3. A rectangular loop sides 10 cm and 3cm moving out of a region of uniform magnetic filed of 0.5T directed normal to the loop. If we want to move loop with a constant velocity 1 cm/sec. then required mechanical force is (Resistance of loop =  $1 \text{m}\Omega$ ) :-



- (1)  $2.25 \times 10^{-3} \text{ N}$
- (2)  $4.5 \times 10^{-3} \text{ N}$
- (3)  $9 \times 10^{-3} \text{ N}$
- (4)  $1.25 \times 10^{-3} \text{ N}$
- 4. A metallic square wire loop of side 10~cm and resistance  $1~\Omega$  is moved with a constant velocity  $v_0$  in a uniform magnetic field of induction B=2~T as shown in the figure. The magnetic field perpendicular to the plane of the loop. The loop is connected to a network of resistors each of value 3 ohm. The resistance of the lead wires OS and PQ are negligible. What should be the speed of the loop so as to have a steady current of 1~mA in it? Give the direction of current in the loop.



- (1)  $2 \times 10^{-2}$  m/sec., anticlockwise direction
- (2)  $4 \times 10^{-2}$  m/sec., anticlockwise direction
- (3)  $2 \times 10^{-2}$  m/sec., clockwise direction
- (4)  $4 \times 10^{-2}$  m/sec. , clockwise direction
- 5. Figure shows a square loop of side 5 cm being moved towards right at a constant speed of 1cm/sec. The front edge just enters the 20 cm wide magnetic field at t=0. Find the induced emf in the loop at t=2s and t=10s.

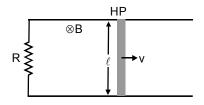


(1)  $3 \times 10^{-2}$ , zero

(2)  $3 \times 10^{-2}$ ,  $3 \times 10^{-4}$ 

(3)  $3 \times 10^{-4}$ .  $3 \times 10^{-4}$ 

- (4)  $3 \times 10^{-4}$ , zero
- 6. A conducting rod moves towards right with constant velocity v in unifrom transverse magnetic field. Graph between force applied by the external agent v/s velocity and power supplied by the external agent v/s velocity.



(1) St. line, parabola

(2) Parabola, st. line

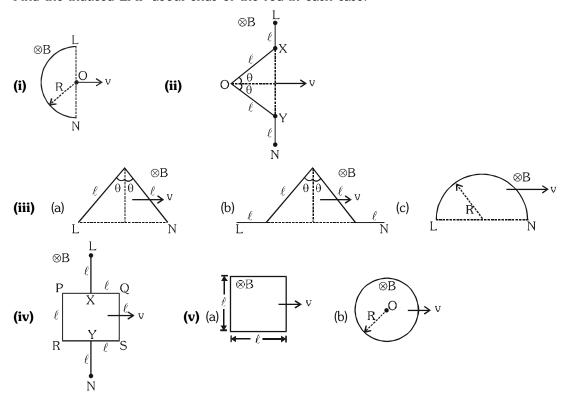
(3) St. line, St. line

(4) Parabola, Parabola

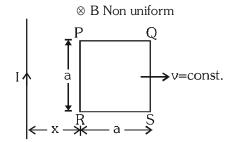


9810934436, 8076575278, 8700391727

7. Find the induced EMF about ends of the rod in each case.



8. Find the EMF induced in metal loop when it moves in non-uniform magnetic field



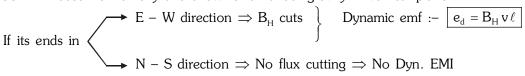
### MOVING CONDUCTING ROD IN EARTH'S MAGNETIC FIELD

(Assume angle of declination is zero)

Case-I Placed Horizontally and moves in horizontal plane.

Case-II Hold vertically and moves in horizontal plane:-

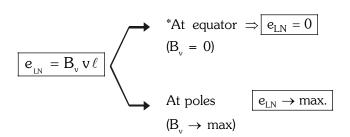
Case-III Placed horizontally and allow to fall under gravity in vertical plane :-

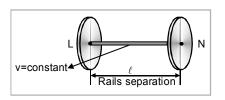




# • Applications (Hz $\rightarrow$ Horizontal, $V_t \rightarrow$ vertical)

(i) Moving Train (Hz - Hz) :- Induced emf across axle of moving train is :-

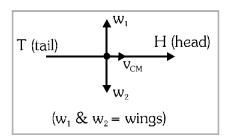




where  $B_v = B\sin\theta$ ,  $\theta$  angle of dip at that place  $v \rightarrow m/sec$ .

## (ii) Moving Aeroplane:

Motion of aeroplane can be deal as motion of two metal rods (H-T) and  $(w_1-w_2)$  which are perpendicular to each other. For (H-T) conductor  $\vec{\ell} \mid \mid \vec{v}_{cm}$ , so (H-T) condutor never do flux cutting hence no induced emf across (H-T) of aeroplane for its any sort of motion, only  $(w_1-w_2)$  conductor can do flux cutting.



# (a) When aeroplane flying at a certain height ie parallel to earth surface (Hz - Hz) :

Induced emf across wings of aeroplane given as (both cases) :-

$$e_{w_1w_2} = B_v \ell_{w_1w_2} v$$
, where  $B_v = B \sin\theta$  [ $\theta$  angle of dip.]

# (b) When aeroplane dives vertically (Hz - Vt) :-

If wings 
$$(w_1-w_2)$$
 in 
$$N-S \ direction \Rightarrow B_H \ cuts$$
 N - S direction  $\Rightarrow$  No flux cutting  $\Rightarrow$  No Dy. EMI

Induced emf across wings of aeroplane given as (only in one case)

$$\boxed{e_{w_1w_2} = B_H \, \ell_{w_1w_2} \, v} \;, \quad \text{where } B_H = B cos \theta \quad [\theta \text{ angle of dip.}]$$

### (iii) Human body (Vt - Hz):

A human body of height 'h' moves with constant velocity v then induced

emf between his head and feet, if it moves along:

$$ightharpoonup E - W line  $\Rightarrow B_H \text{ cuts}$  Dynamic emf  $\Rightarrow e_d = B_H \text{vh}$   
 $ightharpoonup N - S line  $\Rightarrow No \text{ flux cutting} \Rightarrow No \text{ Dyn. EMI}$$$$





# INDUCED E.M.F. DUE TO ROTATION OF A CONDUCTOR ROD IN A UNIFORM MAGNETIC FIELD

Let a conducting rod is rotating in a magnetic field around an axis passing through its one end, normal to its plane.

Consider an small element dx at a distance x from axis of rotation.

Suppose velocity of this small element = v

So, according to Lorent's formula induced e.m.f. across this small element

$$d\epsilon = B v. dx$$

: This small element dx is at distance x from O (axis of rotation)

 $\therefore$  Linear velocity of this element dx is v =  $\omega\,x$ 

substitute of value of v in eq<sup>n</sup> (i)  $d\varepsilon = B \omega x dx$ 

Every element of conducting rod is normal to magnetic field and moving in perpendicular direction to the field

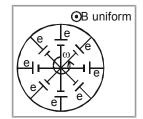
So, net induced e.m.f. across conducting rod 
$$\ \epsilon = \int d\epsilon = \int\limits_0^\ell B\omega \ x \ dx = \omega \ B \bigg( \frac{x^2}{2} \bigg)_0^\ell$$

$$\begin{array}{lll} \text{or} & & \epsilon = \frac{1}{2}B \quad \omega \quad \ell^2 & & \epsilon = \frac{1}{2}B \times 2\pi f \times \ell^2 \quad [f = \text{frequency of rotation}] \\ & = B \ f \ (\pi \ \ell^2) & & \text{area traversed by the rod } A = \pi \ \ell^2 & \text{or} & \epsilon = B \end{array}$$



- During rotational motion of disc it cuts the magnetic flux.
- A metal disc can be assumed to made of uncountable radial conductors. When metal disc rotates in uniform transverse magnetic field these radial condutors cuts the magnetic flux and because of this flux cutting all becomes identical cells each of emf 'e', where  $e=\frac{1}{2}B\omega R^2$ , as shown in following figure and periphery of disc becomes equipotential.
- ullet All identical cells connected in parallel fashion so net emf  $e_{\rm net} = e$  (emf of single cell)

$$\label{eq:energy} \boxed{ \begin{aligned} e_{\text{net}} &= \frac{1}{2}B\omega R^2 \\ \omega &= 2\pi f \end{aligned}} \text{, where } R \text{ is radius of disc.}$$

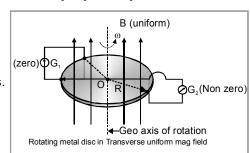


- Net induced emf between centre and rim of disc is  $\frac{1}{2}B\omega R^2$ .
- Reading of Galvanometers :-

G-1:- Its reading is zero if it is connected between any two peripherial points or diametrical opposite. ends.

G-2: Its reading is non zero if it is is connected between centre and peripherial point.

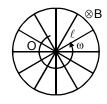
Faraday Copper disc generator (Based on Dynamic EMI): When disk rotates about its axis perpendicular to magnetic
 field then emf induces about its center and peripheral points.





### Illustration 20.

A conducting cycle wheel with each spoke of length  $\ell$ , is rotating about its geometrical axis with uniform angular velocity  $\omega$  in uniform magnetic field as shown in figure. Find induced emf between its centre and rim.



## Solution.

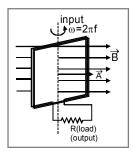
Due to flux cutting each metal spoke becomes identical cell of emf e (say), all such identical cells connected in parallel fashion  $e_{net} = e$  (emf of single cell)

$$e_{net} = \frac{1}{2}B\omega\ell^2$$
$$\omega = 2\pi f$$

Sp. Note: This emf does not depends on number of spokes ('N') in wheel.

# **12. PERIODIC E.M.I.** $\left[\frac{d\theta}{dt} \rightarrow \frac{d\phi}{dt}\right]$

When a coil, which is placed in uniform magnetic field, rotates with constant angular frequency about shown axis then magnetic flux through the coil changes periodically with respect to time so an emf of periodic nature induced in coil. This phenomenon known as periodic emi.



• Magnetic flux through the rotating coil at any instant 't' :-

$$\phi = NBA \cos\theta = NBA \cos\omega t$$
 (as  $\theta = \omega t$ )

$$\boxed{\phi = \phi_0 \cos \omega t}$$
 where  $\boxed{\phi_0 = NBA}$   $\Rightarrow$  flux amplitude or max. flux

 $\textbf{Sp. Note:-} \ \text{Magnetic flux changes periodically with respect to time.}$ 

• Induced emf in rotating coil at any instant 't' :-

$$e = -\frac{d\phi}{dt} = NBA\omega sin\omega t$$

$$e=e_0\sin\omega t$$
 , where  $e_0=NBA\omega=\phi_0\omega$   $\Rightarrow$  emf amplitude or max. emf

• Induced current in load circuit at any instant 't' :-

$$I = e/R = \frac{e_0}{R} \sin \omega t$$

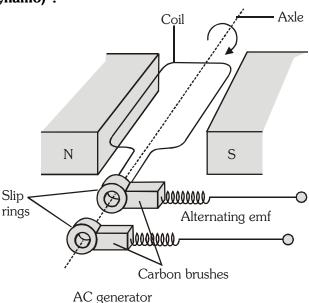
$$\overline{ I = I_0 \sin \omega t } \ , \ \ \text{where} \ \ \overline{ I_0 = \frac{e_0}{R} = \frac{NBA\omega}{R} = \frac{\phi_0 \omega}{R} } \ \Rightarrow \ \ \text{Current Amplitude or max. current}$$

- Induced emf also changes in periodic manner thats why this phenomenon called periodic EMI.
- Phase difference between magnetic flux through the coil and induced emf is 90°.
  - (a) When plane of coil perpendicular to  $\vec{B} \Rightarrow \phi_{max}$  and  $e_{min} = 0$
  - **(b)**When plane of coil parallel to  $\vec{B} \, \Longrightarrow \, \varphi_{\text{min}} = \, 0$  and  $e_{\text{max}}$
- Induced emf and current acquires their max and min values simultaneously ie phase difference between both induced parameters is zero.
- Frequency of induced parameter = Rotational frequency of coil = f.
- Induced emf and current changes their value with respect to time according to sine function, hence they called as sinusoidal induced quantities

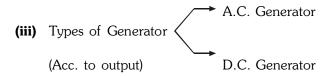


### 13. MAIN APPLICATIONS OF E.M.I.:

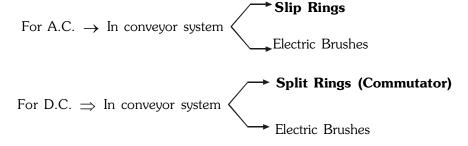
- (A) Generator (G)  $\rightarrow$  Based on periodic EMI
- (B) DC Motor
- (C) Transformer (T)  $\rightarrow$  Based on Mutual induction (Static EMI)
- Sp. points :-
- (a) There is no mechanical losses for transformer, because it has no moving element and hence efficiency of transformer is higher than Generator and motor.
- (b) Common losses for Generator and transformer
  - (i) Joule heating losses or Cu losses
  - (ii) Iron losses: (a) Eddy currents losses (b) Hysteresies losses
  - (iii) Flux leakage losses
- (A) Generator (or Dynamo) :-



- (i) Work: It converts mechanical energy into electrical energy.
- (ii) Working principle  $\rightarrow$  Periodic E.M.I.



- (iv) Generator has basic three sections
  - (a) Armature circuit (Internal circuit)
  - (b) Conveyor system (Connector of two circuit)
  - (c) Load circuit (External circuit)
- (v) Basic difference between A.C. G. and D.C. G. in conveyor system.





# **GOLDEN KEY POINTS**

## Special chart For Rotating coil

	Phy. parameter	Equation	Max value	Frequency $(f = \omega/2\pi)$
(a)	Magnetic flux	$\phi = \phi_0 \cos \omega t$	$\phi_0 = NBA$	f
(b)	Induced emf	$e = e_0 \sin \omega t$	$e_0 = NBA\omega$	f
(c)	Induced current	$I = I_0 \sin \omega t$	$I_0 = \frac{NBA\omega}{R}$	f

Ν

## (B) DC Motor:

- It's a device, that converts electrical energy into mechanical energy (rotational energy).
- Principle: When current carrying coil is placed in magnetic field it experiences a torque.
- Working: When DC motor is connected to a dc source, a current flow in coil, which reverses it direction in regular intervals so that magnetic torque act on coil in same direction. The direction of current is reversed by commutator. Due to rotation of coil in magnetic field, magnetic flux linked with coil changes with time hence E.M.F. is induced, which opposes the current in the coil. This e.m.f. is known as back emf.

If coil of N turns, each of area A rotates with constant angular velocity. Then peak value of back e.m.f. is given by:

$$e_0 = NBA\omega$$
  
i.e.  $e_0 \propto \omega$ 

i.e. 
$$e_0 \propto \omega$$

Equation of motor (D.C.):

$$E - e = iR$$

At t = 0, when motor is switched ON,  $\omega = 0$ 

$$\Rightarrow$$
  $e = 0$  and  $i = \frac{E}{R} = Maximum$ 

as 
$$t\uparrow$$
,  $\omega\uparrow\Rightarrow e\uparrow$  but  $i\downarrow$ 

and when motor rotate with maximum angular speed, current is minimum.

$$i_{min} = \frac{E - e_{max\,imum}}{R}$$

Efficiency of motor:

$$\eta = \frac{P_{out}}{P_{\cdot}} \times 100 = \frac{ei}{Ei} \times 100$$

$$\eta = \frac{e}{E} \times 100$$

**Note:** When  $e = \frac{E}{2}$ , then efficiency of motor is maximum.

$$\eta_{maximum} = 50\%$$



Armature

Commutator

# Illustrations

#### Illustration 21.

A circular coil of radius 8.0 cm and 20 turns rotates about its vertical diameter with an angular speed of  $50\,\mathrm{s^{-1}}$  in a uniform horizontal magnetic field of magnitude  $3\times10^{-2}\,\mathrm{T}$ . Obtain the maximum and average induced emf in the coil. If the coil forms a closed loop of resistance  $10\,\Omega$ , how much power is dissipated as heat ? What is the source of this power ?

#### **Solution**

Induced emf in coil:-

 $e = NBA\omega sin\omega t$ 

$$e_{max} = NBA\omega = NB(\pi r^2)\omega = 20 \times 3.0 \times 10^{-2} \times \pi \times 64 \times 10^{-4} \times 50 = 0.603 \text{ V}$$

e<sub>avo</sub> is zero over a one cycle

$$I_{\text{max}} = \frac{e_{\text{max}}}{R} = \frac{0.603}{10} = 0.0603 \text{ A}$$

$$P_{\text{avg}} = \frac{I_{max}^2 R}{2} = 0.018W$$

The induced current causes a torque opposing the rotation of the coil. An external agent (rotor) must supply torque (and do work) to counter this torque in order to keep the coil rotating uniformly. Thus, the source of the power dissipated as heat in the coil is the external rotor.

### Illustration 22.

An a.c. generator consists of a coil of 50 turns and area 2.5 m<sup>2</sup> rotating at an angular speed of 60 rad  $sec^{-1}$  in a uniform magnetic field B = 0.30 T between two fixed pole pieces. The resistance of the circuit including that of the coil is  $500\Omega$ .

- (a) Calculate the maximum current drawn from the generator.
- (b) What will be the orientation of the coil w.r.t. the magnetic field to have (i) maximum magnetic flux (ii) zero magnetic flux.
- (c) Would the generator work if the coil were stationary and instead the poles were rotated with same speed as above.

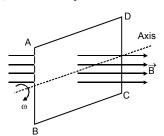
### **Solution**

(a) Maximum Current, 
$$I_{max} = \frac{e_{max}}{R} = \frac{NBA\omega}{R} = \frac{50 \times 0.3 \times 2.5 \times 60}{500} = 4.5A$$

- (b) Flux is maximum, when plane of coil is perpendicular to the magnetic field. Flux is zero when plane of coil is parallel to the magnetic field.
- (c) Yes, it will work.

# **BEGINNER'S BOX-8**

- 1. A rectangular coil ABCD is rotated in uniform magnetic field with constant angular velocity about its one of the diameter as shown in figure. The induced emf will be maximum, when the plane of the coil is :-
  - (1) Perpendicular to the magnetic field
  - (2) Making an angle of 30° with the magnetic field.
  - (3) making an angle of 45° with the magnetic field.
  - (4) Parallel to the magnetic field.



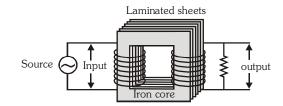


- 2. A rectangular coil has 60 turns and its length and width is 20 cm and 10 cm recpectively. The coil rotates at a speed of 1800 rotation per minute in a uniform magnetic field of 0.5 T about its one of the diameter. The maximum induced emf will be :-
  - (1) 98 V
- (2) 110 V
- (3) 113 V

(4) 118 V

### (C) TRANSFORMER

- **Working principle :-** Mutual induction (i)
- Transformer has basic two section :-(ii)



- (a) Shell: It consist of primary and secondary coils of copper. The effective resistance between primary and secondary coil is infinite because electric circuit between two is open ( $R_{ps} = \infty$ )
- (b) Core: Both Cu coils are tightly wound over a bulk metal piece of high magnetic permeability (eq. soft iron) called core. Both coils are electrically insulated to core but core part magnetically coupled to both the coils.
- (iii) Work: - It regulates A.C. voltage and transfers the electrical electrical power without change in frequency of input supply. (The alternating current changes itself.)
- (iv) Special Points :-
  - It can't work with D.C. supply. If a battery is connected to its primary then output is across scondary is always zero ie. No working of transformer.
  - It can't called 'Amplifier' as it has no power gain like **transistor**.
  - It has no moving part hence there are no mechanical losses in transformer, so its efficiency is higher than generator and motor.
- (v) **Types** (According to voltage regulation) :-

$$\begin{tabular}{lll} \textbf{Type} & & \\ \hline & Step up transformer & (S.U.T), & N_{_{S}} > N_{_{P}} \\ \\ & & \\ \hline & Step down transformer & (S.D.T) & N_{_{S}} < N_{_{P}} \\ \\ \hline \end{tabular}$$

- (vi) S.U.T. ⇒ converts low voltage, high current in to high voltage, low current
  - S.D.T. ⇒ converts high voltage, low current into low voltage, high current.
- Power transmission is carried out always at "High voltage, low current" so that voltage drop and (vii) power losses are minimum in transmission line.

- Sending power always at high voltage & low current (By. S.U.T.) and Recieving power always (viii) at low voltage & high current (By S.D.T.)
- (ix) High voltage coil having more number of turns and always made of thin wire and high current coil having less number of turns and always made of thick wires.



- Ideal Transformer :  $(\eta = 100\%)$ (x)
  - No flux leakage:-

$$\varphi_{\rm s} \,=\, \varphi_{\rm p} \implies \frac{-d\varphi_{\rm s}}{dt} \,=\, \frac{-d\varphi_{\rm p}}{dt}$$

 $e_s = e_p = e$  induced emf per turn of each coil is also same.

total induced emf for secondary  $E_s = N_s e$ total induced emf for primary  $E_p = N_p e$ 

$$\frac{E_s}{E_p} = \frac{N_s}{N_p} = n \text{ or } p \dots (1) \text{ where } \langle$$

n :turn ratio

p: transformation ratio

(b)

No load condition :- 
$$V_{P} = E_{P} \ \& \ E_{S} = V_{S}$$

$$\boxed{\frac{V_S}{V_P} = \frac{N_S}{N_P}} \qquad \dots (2)$$

$$V_S = \frac{N_S}{N_P} = n \text{ or } p$$
 ..... (3) [ from (1) & (2) ]

(c)

No power loss :- 
$$P_{out} = P_{in} \\ V_{s}I_{s} = V_{p}I_{p}$$

$$\frac{V_S}{V_P} = \frac{I_P}{I_S}$$

from eqn. (3) & (4)

$$\frac{V_S}{V_P} = \frac{I_P}{I_S} = \frac{N_S}{N_P} = n \text{ or } p$$

**Sp. Note:** Generally transformers deals in ideal condition i.e.  $P_{in} = P_{out}$ , if other information are not given.

(xi) **Real transformer (\eta \neq 100\%)**:- Some power is always lost due to flux leakage, hysteresis, eddy currents, and heating of coils. hence  $\boldsymbol{P}_{\text{out}} < \boldsymbol{P}_{\text{in}}$  always.

Efficiency of transformer

$$\eta = \frac{P_{out}}{P_{in}} = \frac{V_S I_S}{V_P I_P} \times 100$$

Losses in Transformer:

Copper or joule heating losses :-(i)

> Where : These losses occurs in both coils of shell part.

Reason : Due to heating effect of current ( $H = I^2Rt$ ).

Remedy : To minimise these losses, high current coil always made up with thick wire and for removal

of produced heat, circulation of mineral oil should be used.

(ii) Flux leakage losses :-

> Where : These losses occurs in between both the coil of shell part.

Cause : Due to air gap between both the coils.

: To minimise these losses both coils are tightly wound over a common soft iron core Remedy

(high magnetic permeability) so a closed path of magnetic field lines formed itself within

the core and tries to makes coupling factor  $K \rightarrow 1$ 

(iii) Iron losses :-

> Where : These losses occurs in core part.

→(i) Hysteresis losses **Types** ► (ii) Eddy currents losses



# (a) Hysteresis losses :-

**Cause** : Transformer core always present in the effect of alternating magnetic field ( $B = B_0 \sin \omega t$ ) so it will magnetised & demagnetised with very high frequeny (f = 50 Hz).

During its demagnetization a part of magnetic energy left inside core part in form of

residual magnetic field. Finally this residual energy waste as heat.

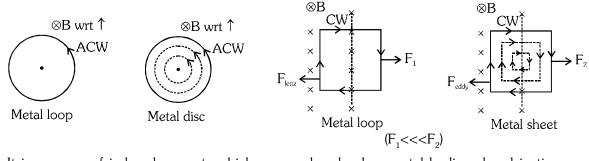
**Remedy** : To minimise these losses material of transformer core should be such that it can be easily magnetised & demagnetised. For this purpose magnetic soft materials should be used.

Ex.: soft Iron

Low coercivity

## (b) Eddy current losses:

# \* Eddy currents (or Focalt's currents) [Experimental verification by focalt]



**Def.:** It is a group of induced currents which are produced, when metal bodies placed in time varying magnetic field or they moves in external magnetic field in such a way that flux through them changes with respect to time.

# **GOLDEN KEY POINTS**

- (i) These currents are produced only in closed path within the entire volume and on the surface of metal body. Therefore their measurement is impossible.
- (ii) Circulation plane of these currents is always perpendicular to the external magnetic field direction.
- (iii) Generally resistance of metal bodies is low so magnitude of these currents is very high.
- (iv) These currents can heat up the metal body and some time body will melt out (Application : Induction furnace)
- (v) Due to these induced currents a strong eddy force (or torque) acts on metal body which always opposes the translatory (or rotatory) motion of metal body, according to Lenz law.
- (vi) Transformer:
  - **Cause** : Transformer core is always present in the effect of alternating magnetic field ( $B = B_0 \sin \omega t$ ).

Due to this eddy currents are produced in its volume, so a part of magnetic energy of

core is wasted as heat.

**Remedy** : To minimise these losses transformer core should be laminated. with the help of lamination process, circulation path of eddy current is greatly reduced & net resistance of system

is greatly increased. So these currents become feeble.

### Applications of eddy currents :-

(i) Induction furnace (ii) Dead beat galvanometer

(iii) Electric Brakes (iv) Induction motor

(v) Car speedometer (vi) Energy meter

# Illustrations -

# Illustration 23.

A power transmission line feeds input power at 2300 V to a step down transformer having 4000 turns in its primary. What should be the number of turns in the secondary to get output power at 230 V?

# Solution

$$V_{p} = 2300 \text{ V} ; N_{p} = 4000, V_{S} = 230 \text{ V}$$

$$\frac{V_{_S}}{V_{_P}} = \frac{N_{_S}}{N_{_P}} \qquad \qquad \therefore \qquad \qquad N_{_S} = N_{_P} \times \frac{V_{_S}}{V_{_P}} = 4000 \times \frac{230}{2300} = 400$$



#### Illustration 24.

The output voltage of an ideal transformer, connected to a 240 V a.c. mains is 24 V. When this transformer is used to light a bulb with rating 24V, 24W calculate the current in the primary coil of the circuit.

#### **Solution**

$$\begin{aligned} &V_{P}=240 \text{ V} &V_{S}=24 \text{ V}, &V_{S} \text{ } I_{S}=24 \text{ W} \end{aligned}$$
 Current in primary coil  $I_{P}=\frac{V_{S}I_{S}}{V_{P}}=\frac{24}{240}=0.1 A$ 

#### **BEGINNER'S BOX-9**

- 1. Why the core of transformer is laminated?
- 2. A step down transformer is used to reduce the main supply of 220 V to 11 V. If the primary coil draws a current of 5A and the current in seondary coil 90A, What is the efficiency of the transformer?
- 3. Why can't transformer be used to step up d.c. voltage?
- 4. Write two applications of eddy currents.

# ANSWERS

### **BEGINNER'S BOX-1**

- **1.**  $5 \times 10^{-3}$  Weber
- **2.** –NBA
- **3.** Face ABCD  $\Rightarrow$  +Ba<sup>2</sup>, Face EFGH  $\Rightarrow$  -Ba<sup>2</sup>, Remaining faces ⇒ Zero
- **5.** -0.1 Wb **4.** 0.02 Wb
- **6.**  $29.6 \times 10^{-6}$  Wb

### **BEGINNER'S BOX-2**

- 1. (i) Anticlockwise
- (ii) Clockwise
- (iii) A Positive charge, B Negative charge
- (iv) Anticlockwise
- (vi) No induced current
- (v) Anticlockwise (vii) (a) Anticlockwise
- (b) Anti clockwise in bigger loop & clockwise in maller loop
- (c) Anti clockwise in bigger loop & clockwise in smaller loop
- (d) Anticlockwise in both loop & through connecting wire zero current

(viii) Anticlockwise

- 2. (i) (a) Anticlockwise (ACW), (b) Clockwise (CW)
  - (ii) N to L
  - (iii) Plate A Positive charge, Plate B Negative charge

#### **BEGINNER'S BOX-3**

- **1.** (4) **2.** (2)
- **3.** (4)
- **4.** (3)

- **5.** (2)
- **6.** (2)
- **7.** (1)
- **8.** (2)

**9.** (2)

#### **BEGINNER'S BOX-4**

- **1.** (3) **2.** (2)
- **3.** (1)
- **4.** (2)

- **5.** (1)
- **6.** (4)
- **7.** (4)

### **BEGINNER'S BOX-5**

- **1.** (4) **5.** (4)
- **2.** (2) **6.** (1)
- **3.** (1)
- **4.** (1)

**9.** (2)

- **7.** (4)
- **8.** (4)

- Shrivastava Classes, D-27, Near JVTS Garden, Chattarpur Extension New Delhi - 110074
  - 9810934436, 8076575278, 8700391727

# **BEGINNER'S BOX-6**

- **1.** (1)
  - **2**. (2)
- **3.** (2)
- **5.** (3)
- **6.** (1)
- **7.** (4)
- 8. (i) (a) ACW, (b) Zero, (c) CW
  - (ii) (a) ACW, (b) Zero, (c) CW
  - (iii) (a) L to N, (b) Zero, (c) N to L

# **BEGINNER'S BOX-7**

- 1. (i) No induced EMF
- (ii) B outwards

**4.** (3)

- (iii) B inwards
- (iv) Direction of current Q to P
- (v) Low potential is N
- (vi) Y south & X north

**4.** (2)

- (vii) X south; Y north
- **2.** (1)
- **3.** (1)
- **6.** (1)
- **5.** (4)
- **7.** (i) 2 BvR, (ii) 2 Bvl  $(1 + \sin \theta)$ , (iii) (a) Zero, (b) Zero, (c) Zero (iv) 3 Bvl (v) (a) Zero; (b) Zero

**8.** 
$$e_{\text{net}} = \frac{\mu_0 \text{Iva}^2}{2\pi v(v + a)}$$

# **BEGINNER'S BOX-8**

**1**. (4) **2.** (3)

# **BEGINNER'S BOX-9**

- 1. To reduce eddy current
- **3.** Working of transformer is based on mutual induction
- **4.** Application of eddy current
  - (i) Induction furnace,
  - (ii) Electric Brakes

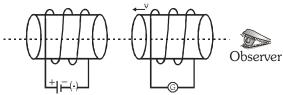
# **EXERCISE-I** (Conceptual Questions)

#### **MAGNETIC FLUX**

- 1. 'SI' unit of magnetic flux is :-
  - (1) ampere/meter<sup>2</sup>
- (2) weber
- (3) gauss
- (4) orested
- A square coil of  $0.01\ m^2$  area is placed 2. perpendicular to the uniform magnetic field of 103 weber/metre<sup>2</sup>. The magnetic flux linked with the coil is :-
  - (1) 10 weber
- (2) 10<sup>-5</sup> weber
- (3) Zero
- (4) 100 weber

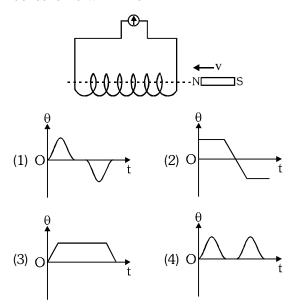
#### **FARADAY LAW & LENZ'S LAW**

- 3. According to Faraday's Laws of electro magnetic induction:
  - (1) The direction of the induced current is such that it opposes it self
  - (2) The induced emf in the coil is proportional to the rate of change of magnetic flux associated with it
  - (3) The direction of induced emf is such that it opposes it self
  - (4) None of the above
- 4. A coil having an area of 2 m<sup>2</sup> is placed in a magnetic field which changes from 1 Weber/m<sup>2</sup> to 4 Weber/m² in 2 seconds. The e.m.f. induced in the coil will be :-
  - (1) 4 volt
- (2) 3 volt
- (3) 2 volt
- (4) 1 volt
- 5. Magnetic field through a coil is changed with respect to time then emf induced in it then select the incorrect regarding induced emf in coil :-
  - (1) Coil may be made up with wood
  - (2) Coil may be connected with an open circuit
  - (3) Coil must be of conducting nature
  - (4) Induced emf does not depends upon resistance of the coil
- 6. The current flows in a circuit as shown below. If a second circuit is brought near the first circuit then the current in the second circuit will be :-



- (1) Clock wise
- (2) Anti clock wise
- (3) Depending on the value of  $R_a$
- (4) None of the above

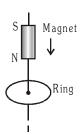
- 7. A coil of resistance  $10\Omega$  and 1000 turns have the magnetic flux line of  $5.5 \times 10^{-4}$  Wb. If the magnetic flux changed to  $5 \times 10^{-4}$  Wb. in 0.1 sec, then the induced charge in coil is :-
  - (1) 50 μC (2) 5 μC
- (3) 2 uC
- (4) 20 µC
- 8. One coil of resistance  $40\Omega$  is connected to a galvanometer of  $160\Omega$  resistance. The coil has radius 6mm and turns 100. This coil is placed between the poles of a magnet such that magnetic field is perpendicular to coil. If coil is dragged out then the charge through the galvanometer is 32µC. The magnetic field is:-
  - (1) 6.55 T
- (2) 5.66 T
- (3) 0.655 T
- (4) 0.566 T
- 9. A short bar magnet passes at a steady speed right through a long solenoid. A galvanometer is connected across the solenoid. Which graph best represents the variation of the galvanometer deflection  $\theta$  with time :-



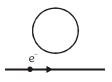
- A square loop of side 22 cm is changed to a circle in time 0.4 s. The magnetic field present is 0.2 T. The emf induced is :-
  - (1) -6.6 mV
- (2) -13.2 mV
- (3) +6.6 mV
- (4) +13.2 mV
- The magnetic flux in a coil of 100 turns increases by  $12 \times 10^3$  Maxwell in 0.2 s due to the motion of a magnet. The emf induced in the coil will be:-
  - (1) 0.6 mV (2) 0.6 V
- (3) 6 V
- (4) 60 V



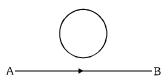
- 12. A closed coil consists of 500 turns on a rectangular frame of area 4.0 cm<sup>2</sup> and has a resistance of 50 ohms. The coil is kept with its plane perpendicular to a uniform magnetic field of 0.2 wb/m<sup>2</sup>, the amount of charge flowing through the coil if it is turned over (rotated through 180°):-
  - (1)  $1.6 \times 10^{-3}$  C
  - (2)  $16 \times 10^{-3}$  C
  - (3)  $0.16 \times 10^{-3}$  C
  - (4)  $160 \times 10^{-3}$  C
- **13.** A coil of mean area 500 cm<sup>2</sup> and having 1000 turns is held perpendicular to a uniform field of
  - 0.4 gauss. The coil is turned through  $180^{\circ}$  in
  - $\frac{1}{10}$  second. The average induced e.m.f. :-
  - (1) 0.04 V
- (2) 0.4 V
- (3) 4 V
- (4) 0.004 V
- 14. An emf induced in a coil, the linking magnetic flux
  - (1) Must decrease
  - (2) Must increase
  - (3) Must remain constant
  - (4) Can be either increased or decreased
- 15. Consider a metal ring kept on a horizontal plane. A bar magnet is held above the ring with its length along the axis of the ring. If the magnet is dropped freely the accelration of the falling magnet is (g is accelration due to gravity):-



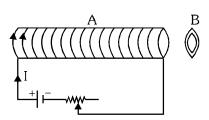
- (1) More than g
- (2) Equal to g
- (3) Less than g
- (4) Depend on mass of magnet
- **16.** An electron beam is moving near to a conducting loop then the induced current in the loop:
  - (1) clockwise
  - (2) anticlockwise
  - (3) both
  - (4) no current



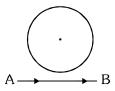
**17.** The current flows from A to B as shown in the figure. The direction of the induced current in the loop is :-



- (1) clockwise
- (2) anticlockwise
- (3) straight line
- (4) none of these
- **18.** Faraday law represents :-
  - (1) relation between I and B
  - (2) relation between magnetic force and magnetic field
  - (3) relation between e.m.f and rate of change of flux
  - (4) none of these
- **19.** An aluminium ring B faces an electromagnet A. The current I through A can be altered. Then which of the following statement is correct:



- (1) If I decreases A will repel B
- (2) Whether I increases or decreases, B will not experience any force
- (3) If I increases, A will repel B
- (4) If I increases, A will attract B
- **20.** A charge particle moves along the line AB, which lies in the same plane of a circular loop of conducting wire as shown in the fig. Then:



- (1) No current will be induced in the loop
- (2) The current induced in the loop will change its direction as the charged particle passes by
- (3) The current induced will be anticlockwise
- (4) The current induced, will be clockwise



- 21. The magnetic flux through a circuit of resistance R changes by an amount  $\Delta \phi$  in a time  $\Delta t$ . The total quantity of electric charge Q that passes any point in the circuit during the time  $\Delta t$  is represented by:-
  - (1) Q =  $\frac{\Delta \phi}{R}$
- $(2) Q = \frac{\Delta \phi}{\Lambda +}$
- (3)  $Q = R \cdot \frac{\Delta \phi}{\Delta t}$  (4)  $Q = \frac{1}{R} \cdot \frac{\Delta \phi}{\Delta t}$
- **22**. If number of turns of 70cm<sup>2</sup> coil is 200 and it is placed in a magnetic field of 0.8 Wb/m<sup>2</sup> which is perpendicular to the plane of coil and it is rotated through an angle 180° in 0.1 sec, then induced emf in coil :-
  - (1) 11.2 V (2) 1.12 V (3) 22.4 V (4) 2.24 V
- A circular loop of radius r is placed in a region where magnetic field increases with respect to time as B(t) = at then induced emf in coil :-
  - (1)  $\pi r^2 a$
- (2)  $3\pi r^2 a$
- (3)  $2\pi r^2 a$
- (4)  $4\pi r^2 a$
- **24.** A circular loop of radius r is moved away from a current carrying wire then induced current in circular loop

will be :-

- (1) Clock wise
- (2) Anti clockwise
- (3) Not induced
- (4) None of them



# SELF INDUCTION AND L-R DC CIRCUIT

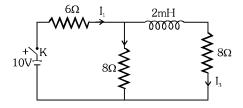
- **25**. When the current through a solenoid increases at a constant rate, the induced current.
  - (1) is a constant and is in the direction of the inducing current
  - (2) is a constant and is opposite to the direction of the inducing current
  - (3) increase with time and is in the direction of the inducing current
  - (4) increase with time and opposite to the direction of the inducing current
- **26**. A solenoid of 10 henry inductance and 2 ohm resistance, is connected to a 10 volt battery. In how much time the magnetic energy will be reaches to 1/4 th of the maximum value?
  - (1) 3.5 sec
- (2) 2.5 sec
- (3) 5.5 sec
- (4) 7.5 sec

- **27**. An inductance coil have the time constant 4 sec, if it is cut into two equal parts and connected parallel then new time constant of the circuit :-
  - (1) 4 sec
- (2) 2 sec
- (3) 1 sec
- (4) 0.5 sec
- 28. Which statement is correct from following -
  - (a) Inductor store energy in the form of magnetic field
  - (b) Capacitor store energy in the form of electric field
  - (c) Inductor store energy in the form of electric and magnetic field both
  - (d) Capacitor store energy in the form of electric and magnetic field both
  - (1) a, b
- (2) a, c
- (3) b, d
- (4) b, c
- **29**. If a current of 2A give rise a magnetic flux of  $5 \times 10^{-5}$  weber/turn through a coil having 100 turns, then the magnetic energy stored in the medium surrounding by the coil is :-
  - (1) 5 joule
- (2)  $5 \times 10^{-7}$  joule
- (3)  $5 \times 10^{-3}$  joule
- (4) 0.5 ioule
- **30**. For a solenoid keeping the turn density constant its lenght makes halved and its cross section radius is doubled then the inductance of the solenoid increased by :-
  - (1) 200%
- (2) 100%
- (3) 800%
- (4) 700%
- 31. A constant current i maintained in a solenoid. Which of the following quantities will increase if an iron rod is inserted in the solenoid along its axis:-
  - (a) Magnetic field at the centre
  - (b) Magnetic flux linked with the solenoid
  - (c) Self inductance of the solenoid
  - (d) Rate of Joule heating
  - (1) a, b, c (2) c, d
- (3) a, b
- (4) Only b
- **32**. The inductance of a solenoid is 5 henery and its resistance is  $5\Omega$ . If it is connected to a 10 volt battery then time taken by the current to reach 9/10<sup>th</sup> of its maximum will be :-
  - (1) 4.0 s
- (2) 2.3 s
  - (3) 1.4 s
- (4) 1.2 s
- 33. An LR circuit with a battery is connected at t = 0. Which of the following quantities is not zero just after the connection :-
  - (a) Current in circuit
  - (b) Magnetic potential energy in the inductor
  - (c) Power delivered by the battery
  - (d) Emf induced in the inductor
  - (1) a, b (2) a, c
- (3) c, d
- (4) Only d

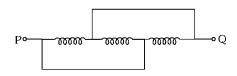


- **34.** During 0.1 s current in a coil increases from 1A to 1.5 A. If inductance of this coil is  $60 \mu H$ , induced current in external resistance of 600  $\mu\Omega$  is :-
  - (1) 1A

- (2) 4/3 A (3) 2/3 A (4) 1/2 A
- **35.** In the circuit shown in figure what is the value of  $I_1$  just after pressing the key K?



- (1)  $\frac{5}{7}$  A
- (2)  $\frac{5}{11}$  A
- (3) 1A
- (4) None of the above
- **36.** Pure inductors each of inductance 3 H are connected as shown. The equivalent induction of the circuit is :-



- (1) 1H
- (2) 2H
- (3) 3H
- (4) 9H
- The time constant of an iductance coil is  $2.0 \times 10^{-3}$  s. When a 90  $\Omega$  resistance is joined in series, the time constant becomes  $0.5 \times 10^{-3}$  s. The inductance and resistance of the coil are :-
  - (1) 30 mH; 30  $\Omega$
- (2) 30 mH;  $60\Omega$
- (3)  $60 \text{ mH} ; 30\Omega$
- (4) 60 mH ;  $60 \Omega$
- **38.** A toroidal solenoid with an air core has an average radius of 15 cm, area of cross-section 12 cm<sup>2</sup> and 1200 turns. Ignoring the field variation across the cross-section of the toroid, the self-inductance of the toroid is :-
  - (1) 4.6 mH
- (2) 6.9 mH
- (3) 2.3 mH
- (4) 9.2 mH
- **39.** A cylindrical iron core supports N turns. If a current I produces a magnetic flux  $\phi$  across the core's cross section, then the magnetic energy is :-
  - (1) I<sub>\phi</sub>
- (2)  $\frac{1}{2}$  I $\phi$  (3)  $\frac{I^2 \phi}{2}$  (4)  $I^2 \phi$

- The self inductance of a toroid is :-
  - (1)  $\frac{\mu_0 N^2 r^2}{2 R_m}$
- (2)  $\frac{\mu_0 N^2 \pi r}{2R_m}$
- (3)  $\frac{\mu_0 N^2 r}{2R_m}$
- (4)  $\frac{\mu_0 N^2 r \pi}{R}$
- 41. An inductance L and a resistance R are joined to a battery. After some time, battery is disconnected but L and R remains connected to the closed circuit. The current strength will be reduced to 37% of its initial value in:
  - (1) RL sec
- (2) R/L sec
- (3) L/R sec
- (4) 1/LR sec
- **42**. Energy is stored in the choke coil in the form of:-
  - (1) Heat
- (2) Electric field
- (3) Magnetic field
- (4) Electro-magnetic field
- When a current changes from 2A to 4A in **43**. 0.05 sec. in a coil, induced emf is 8 V. The self inductance of coil is :-
  - (1) 0.1 H
- (2) 0.2 H
- (3) 0.4 H
- (4) 0.8 H
- An e.m.f. of 12 V is induced in a given coil when the current in it changes at the rate of 48 amp./min. The inductance of the coil is :-
  - (1) 0.5 henry
- (2) 15 henry
- (3) 1.5 henry
- (4) 9.6 henry
- **45**. Two conducting coils are placed co-axially now a cell is connected in one coil then they will :-
  - (1) attract to each other
  - (2) repel to each other
  - (3) both (1) & (2)
  - (4) they will not experience any force
- A coil of resistance  $10\Omega$  and an inductance 5H**46**. is connected to a 100 volt battery. Then energy stored in the coil is :-
  - (1) 125 erg
- (2) 125 J
- (3) 250 erg
- (4) 250 J
- **47**. The energy density in magnetic field B is proportional to :-

  - (1)  $\frac{1}{R}$  (2)  $\frac{1}{R^2}$
- (3) B
- (4)  $B^2$

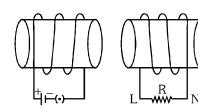


- 48. Inductance of a solenoid is 3H and it consist of 500 turns. If number of turn make twice, then the value of self inductance becomes:-
  - (1) 1.5 H
- (2) 3 H
- (3) 9 H
- (4) 12 H
- **49.** A coil of 40 henry inductance is connected in series with a resistance of 8 ohm and the combination is joined to the terminals of a 2 volt battery. The time constant of the circuit is :-
  - (1)  $\frac{1}{5}$  sec
- (3) 20 sec
- (4) 5 sec
- **50**. When current in a coil is reduced from 2A to 1A in 1 ms, the induced emf is 5V. The inductance of coil is:
  - (1) 5 H
- (2) 5000 H
- (3) 5 mH
- (4) 50 H
- **51.** A coil of inductance 300mH and resistance  $2\Omega$ is connected to a source of voltage 2V. The current reaches half of its steady state value in:-
  - (1) 0.3 s
- (2) 0.15 s
- (3) 0.1 s
- (4) 0.05 s
- **52.** An ideal coil of 10H is connected in series with a resistance of  $5\Omega$  and a battery of 5V. 2 seconds after the connection is made, the current flowing in amperes in the circuit is :-
  - (1) e

- (2) e-1
- $(3) (1-e^{-1})$
- (4) (1-e)

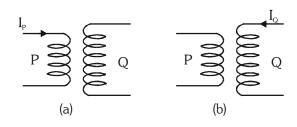
### MUTUAL INDUCTION, TRANSFORMER AND **EDDY CURRENTS**

Two co-axial solenoids shown in figure. If key of primary suddenly opened then direction of instantaneous induced current in resistance 'R' which connected in secondary:



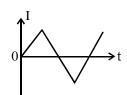
- (1) L to N
- (2) N to L
- (3) Alternating
- (4) Zero

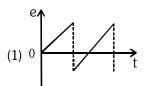
In figure (a) and figure (b) two air-cored solenoids P and Q have been shown. They are placed near each other. In figure (a), when I<sub>D</sub>, the current in P, changes at the rate of 5 As<sup>-1</sup>, an emf of 2 mV is induced in Q. The current in P is then switched off, and a current changing at 2 A s<sup>-1</sup> is fed through Q as shown in diagram. What emf will be induced in P:-

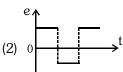


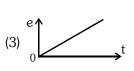
- $(1) 8 \times 10^{-4} \text{ V}$
- (2)  $2 \times 10^{-8} \text{ V}$
- (3)  $5 \times 10^{-3} \text{ V}$
- (4)  $8 \times 10^{-2} \text{ V}$
- **55.** A small square loop of wire of side  $\ell$  is placed inside a large square loop of wire of side L (L >>  $\ell$ ). The loops are coplanar and their centres coincide. The mutual inductance of the system is proportional to:-

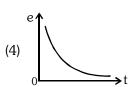
- (1)  $\frac{\ell}{L}$  (2)  $\frac{\ell^2}{L}$  (3)  $\frac{L}{\ell}$  (4)  $\frac{L^2}{\ell}$
- **56**. A current time curve is shown in the following diagram. This type of current is passed in the primary coil of transformer. The nature of induced emf in the secondary coil will be :-













- **57.** Two coil have a mutual inductance 0.005 H. The current changes in first coil according to equation  $I = I_0 \sin \omega t$ , where  $I_0 = 2A$  and  $\omega = 100\pi$  rad/sec. The maximum value of induced emf in second coil is :-
  - (1)  $4\pi V$
- (2)  $3\pi V$
- (3)  $2\pi V$
- (4)  $\pi$  V
- **58**. The electric power is transferred to a far distance at high potential because:-
  - (1) It stops the wire theft
  - (2) To minimise power loss
  - (3) Generator gives only high potential
  - (4) Electric power is transferred early due to high potential
- **59.** If primary winding of a transformer were connected to a battery, the current in it will:
  - (1) Increase
  - (2) Remain constant
  - (3) Decrease
  - (4) First (1) then (3)
- 60. Which type of losses does not occur in transformer:-
  - (1) mechanical losses
  - (2) copper losses
  - (3) hysteresis losses
  - (4) eddy current losses
- The efficiency of a transformer is maximum, **61**. because :-
  - (1) No part of the transformer is in motion
  - (2) It creates maximum voltage
  - (3) It creates minimum voltage
  - (4) None of the above
- **62.** In order to avoid eddy currents in the core of a
  - (1) The number of turns in the secondary coil is made considerably large
  - (2) A laminated core is used
  - (3) A step down transformer is used
  - (4) A high voltage alternating weak current is used
- The mutual inductance of two coils when magnetic flux changes by  $2 \times 10^{-2}$  Wb and current changes by 0.01 A is :-
  - (1) 2 H
- (2) 3 H
- (3) 4 H
- (4) 8 H

- Primary winding and secondary winding of a transformer has 100 and 300 turns respectively. If its input power is 60 W then output power of the transformer will be:-
  - (1) 240 W
- (2) 180 W
- (3) 60 W
- (4) 20 W
- **65**. The ratio of the secondary to the primary turns in a transformer is 3:2 and the output power is P. Neglecting all power losses, the input power must be :-
  - (1)  $\frac{P}{2}$

- (2) P (3)  $\frac{2P}{3}$  (4)  $\frac{3P}{2}$
- 66. Mutual inductance of two coils depends on their self inductance  $L_1$  and  $L_2$  as :-
  - $(1) M_{12} = L_1/L_2$
- (2)  $M_{12} = L_2/L_1$
- (3)  $M_{12} = \sqrt{L_1 L_2}$  (4)  $M_{12} = \sqrt{L_1 / L_2}$
- 67. In transformer, power of secondary coil is:-
  - (1) less than primary coil
  - (2) more than primary coil
  - (3) more in step up and less in step down than primary coil
  - (4) more in step down and less in step up than primary coil
- **68**. If the input voltage of a transformer is 2500 volts and output current is 80 ampere. The ratio of number of turns in the primary coil to that in secondary coil is 20: 1. If efficiency of transformer is 100%, then the voltage in secondary coil is :
  - (1)  $\frac{2500}{20}$  volt
  - (2)  $2500 \times 20 \text{ volt}$
  - (3)  $\frac{2500}{80 \times 20}$  volt
  - (4)  $\frac{2500 \times 20}{80}$  volt
- **69**. A step up transformer has turn ratio 10:1. A cell of e.m.f. 2 volts is fed to the primary. Secondary voltage developed is :-
  - (1) 20 V
- (2) 10 V
- (3) 2 V
- (4) Zero

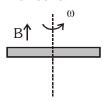
43



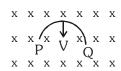
- **70.** The flux linked with a coil at any instant 't' is given by  $\phi = 10t^2 - 50t + 250$ . The induced emf at t = 3 s is :-
  - (1) 190 V
- (2) -190 V
- (3) 10 V
- (4) 10 V
- Two coaxial solenoids are made by winding thin Cu wire over a pipe of cross-sectional area  $A = 10 \text{ cm}^2$  and length = 20 cm. If one of the solenoids has 300 turns and the other 400 turns, their mutual inductance is :-
  - (1)  $2.4 \pi \times 10^{-5} \text{ H}$
- (2)  $4.8 \pi \times 10^{-4} \text{ H}$
- (3)  $4.8 \pi \times 10^{-5} \text{ H}$
- (4)  $2.4 \pi \times 10^{-4} \text{ H}$

### DYNAMIC & ROTATIONAL E.M.F. GENERATOR

**72.** A conducting rod of length  $2\ell$  is rotating with constant angular speed ω about its perpendicular bisector. A uniform magnetic field  $\vec{B}$  exists parallel to the axis of rotation. The emf induced between two ends of the rod is:-

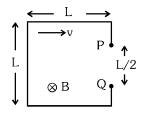


- (1)  $B\omega\ell^2$  (2)  $\frac{1}{2} B\omega\ell^2$  (3)  $\frac{1}{8} B\omega\ell^2$  (4) Zero
- 73. A conducting rod of 1m length rotating with a frequency of 50 rev/sec. about its one of end inside the uniform magnetic field of 6.28 mT. The value of induced emf between end of rod is :-
  - (1) 1 V
- (2) 2 V
- (3) 0.5 V (4) 0.25 V
- **74.** A semicircle loop PQ of radius 'R' is moved with velocity 'v' in transverse magnetic field as shown in figure. The value of induced emf. between the ends of loop is :-



- (1) By  $(\pi r)$ , end 'P' at high potential
- (2) 2 BRv, end P at high potential
- (3) 2 BRv, end Q at high potential
- (4)  $B \frac{\pi R^2}{2} v$ , end P at high potential

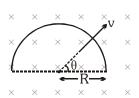
**75**. The loop shown moves with a constant velocity 'v' in a uniform magnetic field of magnitude 'B' directed into the paper. The potential difference between P and Q is 'e':-



- (1)  $e = \frac{BLv}{2}$ , Q is positive with respect to P
- (2)  $e = \frac{BLv}{2}$ , P is positive with respect to Q
- (3) e = 0
- (4) e = BLv, Q is positive with respect to P
- **76**. A conducting wheel in which there are four rods of lengthe  $\ell$  as shown in figure is rotating with angular velocity ω in a uniform magnetic field B. The induced potential difference between its centre and rim will be:



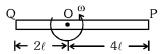
- (1)  $2B\omega\ell^2$
- (2)  $\sqrt{B\ell^2\omega}$
- (3)  $\frac{B\ell\omega}{2}$
- (4)  $\frac{B\ell^2\omega}{2}$
- **77**. A semi circular loop of radius R is placed in a uniform magnetic field as shown. It is pulled with a constant velocity. The induced emf in the loop is:



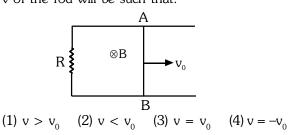
- (1) Bv (πR) cosθ
- (2)  $Bv(pR) sin\theta$
- (3)  $Bv(2R) \cos\theta$
- (4)  $Bv(2R) \sin\theta$



**78.** A conducting rod rotates with a constant angular velocity 'ω' about the axis which passes through point 'O' and perpendicular to its length. A uniform magnetic field 'B' exists parallel to the axis of the rotation. Then potential difference between the two ends of the rod is:



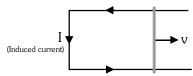
- (1)  $6B\omega\ell^2$ 
  - (2)  $B\omega\ell^2$
- (3)  $10B\omega\ell^2$  (4) Zero
- **79**. Two long parallel metallic wires with a resistance 'R' form a horizontal plane. A conducting rod AB is on the wires shown in figure. The space has magnetic field pointing vertically downwards. The rod is given an initial velocity  $v_0$ . There is no friction in the wires and the rod. After a time 't' the velocity v of the rod will be such that:-



- 80. The armature coil of dynamo is rotating. The generated induced emf varies and the number of magnetic lines of force also varies. Which of the following condition is correct:-
  - (1) lines of flux will be minimum, but induced emf will be zero.
  - (2) lines of flux will be maximum, but the induced emf will be zero.
  - (3) lines of flux will be maximum, but induced emf will be not be zero.
  - (4) the lines of flux will be maximum, and the induced emf will be also maximum.
- A conducting square loop of side  $\ell$  and resistance R moves in its plane with a uniform velocity perpendicular to one of its sides. A uniform and constant magnetic field B exists along the perpendicular to the plane of the loop as shown in the figure. The current induced in the loop is:-
  - (1)  $B\ell v/R$ , clockwise

- (2)  $B\ell v/R$ , anticlockwise  $\begin{array}{c|cccc} x & x & x & x & x & x \\ \hline & x & x & x & x \\ \hline & x & x$
- (4) zero

- If the rotational velocity of a dynamo armature is doubled, then induced e.m.f will become :-
  - (1) half
- (2) two times
- (3) four times
- (4) unchanged
- **83**. Dynamo which produces electricity, is a source of:
  - (1) gravity
- (2) magnetism
- (3) e.m.f.
- (4) electrolysis
- 84. For given arrangement (in horizontal plane) the possible direction of magnetic field:-



- (1) towards right
- (2) towards left
- (3) vertically upward
- (4) vertically downward
- A metallic disc of radius 'R' is rotating about its **85**. geometrical axis with constant angular speed 'w' in external magnetic field B which is perpendicular to the plane of the disc then induced emf between the centre and any peripherical point of the disc is given by :-
  - (1)  $\pi \omega BR^2$  (2)  $\omega BR^2$  (3)  $\frac{\pi \omega BR^2}{2}$  (4)  $\frac{\omega BR^2}{2}$
- **86**. Which of the following is correct for periodic electromagnetic induction :-
  - (1) maximum flux, zero emf
  - (2) zero flux, maximum emf
  - (3) zero flux, zero emf
  - (4) (1) & (2) both
- **87**. Dynamo is based on the principle of :-
  - (1) electro magnetic induction
  - (2) induced current
  - (3) induced magnetism
  - (4) Faraday effect
- 88. Phase difference between induced emf and flux for a coil rotating in magnetic field :-
  - (1) 0
- (2)  $\pi/2$
- $(3) \pi$
- (4)  $2\pi$
- In an AC generator, a coil with N turns, all of the same area A and total resistance R, rotates with frequency  $\omega$  in a magnetic field B. The maximum value of emf generated in the coil is :-

  - (1) NABω (2) NABRω (3) NAB
- (4) NABR



- **90.** The electric generator produce electric current based on which principle :-
  - (1) Ohm's law
  - (2) Faraday's law of EMI
  - (3) Ampere's law
  - (4) Biot savart's law
- **91.** A rectangular loop of sides a & b is placed in magnetic field B. The emf induced in coil when normal of coil makes angle  $\omega t$  with B:-
  - (1) ΒΑωcosωτ
- (2) BAwsinwt
- (3) -BAwsinwt
- (4) -BAωcosωt

### INDUCED ELECTRIC FIELD

**92.** In this given figure if magnetic field increases with time then pattern of induced electric field lines will be:-



- (1) A.C.W. concentric circular field lines in the plane of the paper
- (2) C.W. concentric circular field lines in the plane of the paper
- (3) A.C.W. concentric circular field lines, perpendicular to the plane of the paper
- (4) C.W. concentric circular field lines, perpendicular to the plane of the paper

- **93.** A nonconducting circular ring of radius 4 cm is placed in a time varing magnetic field with rate of 0.2T/s. If 2C charge placed at its circumference then electric force on this charge will be :-
  - (1)  $4 \times 10^{-3} \text{ N}$
- (2)  $8 \times 10^{-3} \text{ N}$
- (3)  $6 \times 10^{-2} \text{ N}$
- (4)  $8 \times 10^{-2} \text{ N}$
- **94.** As a result of change in the magnetic flux linked to the closed loop shown in the figure, an e.m.f. V volt is induced in the loop. The work done (joules) in taking a charge Q coulomb once along the loop is :-



- (1) QV
- (2) QV/2
- (3) 2QV
- (4) Zero

EXERCISE-I	(Conceptual	Questions)

AN	SW	ER	KE	Y

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	2	1	2	2	3	2	2	4	1	1	1	1	1	4	3
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	4	4	3	3	2	1	3	1	1	2	1	1	1	3	2
Que.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans.	1	2	4	4	1	1	3	3	2	1	3	3	2	2	2
Que.	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
Ans.	4	4	4	4	3	3	3	1	1	2	2	4	2	2	1
Que.	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75
Ans.	1	2	1	3	2	3	1	1	4	3	4	4	1	3	2
Que.	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90
Ans.	4	4	1	2	2	4	2	3	4	4	4	1	2	1	2
Que.	91	92	93	94											
			_												



Ans.

# **Directions for Assertion & Reason questions**

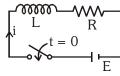
These questions consist of two statements each, printed as Assertion and Reason. While answering these Questions you are required to choose any one of the following four responses.

- (A) If both Assertion & Reason are True & the Reason is a correct explanation of the Assertion.
- **(B)** If both Assertion & Reason are True but Reason is not a correct explanation of the Assertion.
- **(C)** If Assertion is True but the Reason is False.
- **(D)** If both Assertion & Reason are false.
- Assertion: Whenever magnetic flux linked with the coil changes with respect to time, then an emf is induced in it.

**Reason**:— According to lenz law, the direction of induced current in any coil in such a way that it always oposses the cause by which it is produced.

- (1) A
- (2) B
- (3) C
- (4) D
- **2.** Assertion :- Voltage across L (see figure) at t = 0 is E

**Reason :-** Becuase  $E = V_L + V_R$  and at t = 0, i = 0



- (1) A
- (2) B
- (3) C
- (4) D
- **3.** Assertion:—At any instant, if the current through an inductor is zero, then the induced emf may not be zero

**Reason:** An inductor tends to keep the flux (i.e. current) constant

- (1) A
- (2) B
- (3) C
- (4) D
- **4. Assertion**:— Unlike charges are projected in opposite direction in transverse magnetic field, then they are deflected in same directions.

**Reason**:— If a voltmeter connected across two peripherial points of farday copper disc generator, its reading is zero.

- (1) A
- (2) B
- (3) C
- (4) D
- **5. Assertion**:— Faraday's copper disc generator is based on dynamic electromagnetic induction.

**Reason**:— Alternating current generator is based on periodic electromagnetic induction.

- (1) A
- (2) B
- (3) C
- (4) D

- 6. Assertion: When a conducting rod moves in uniform transverse magnetic field with uniform speed which is perpendicular to its length, then potential difference may develop across its ends. Reason: In any conductor, free electrons and free positive ions are available.
  - (1) A
- (2) B
- (3)
- (4) D
- **7. Assertion**:—If a steel core is used in a transformer in place of soft iron core then hyesterisis losses are increased

**Reason**:—Steel core is easily magnetised but it is not easily demagnetised by the alternating magentic field.

- (1) A
- (2) B
- (3) C
- (4) D
- **8. Assertion**: A thin aluminum disc, spinning freely about a central pivot, is quickly brought to rest when placed between the poles of a strong U-shaped magnet.

**Reason**: A current induced in a disc rotating in a magnetic field produces a torque which tends to oppose the disc's motion.

- (1) A
- (2) B
- (3) C
- (4) D
- **9. Assertion:** We use a thick wire in the secondary of a step down transformer to reduce the produced heat.

**Reason:** When the plane of the armature coil is parallel to the line of force of magnetic field, the magnitude of induced e.m.f. is maximum.

- (1) A
- (2) B
- (3) C
- (4) D
- **10.** Assertion: The quantity L/R possesses dimension of time.

**Reason:**—To reduce the rate of growth of current through a solenoid, we should increase the time constant (L/R).

- (1) A
- (2) B
- (3) C
- (4) D
- **11.** Assertion:— An electric field is induced in a closed loop where magnetic field is variable. The induced

E is not a conservative field.

**Reason:-** The line integral  $\vec{E}.d\vec{\ell}$  around the closed loop is non zero.

- (1) A
- (2) B
- (3) C
- (4) D

47



**③** Shrivastava Classes, D-27, Near JVTS Garden, Chattarpur Extension New Delhi - 110074 12. Assertion:- Only a change of magnetic flux with time, will maintain an induced current in the coil.
Reason:- The presence of a large magnetic flux

**Reason:**—The presence of a large magnetic flux will maintain an induced current in the coil.

- (1) A
- (2) B
- (3) C
- (4) D
- **13.** *Assertion:* Self-inductance is called the inertia of electricity.

**Reason:**— In a LR circuit, the inductor opposes any change in current.

- (1) A
- (2) B
- (3) C
- (4) D
- **14. Assertion:** If a charged particle is released from rest in a time varying magnetic field, it moves in a circle.

**Reason:**— In a time varying magnetic field, conservative electric field is induced.

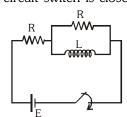
- (1) A
- (2) B
- (3) C
- (4) D
- **15. Assertion:** The possibility of an electric bulb fusing is higher at the time of switch OFF.

**Reason:**—Inductive effects produce a surge at the time of switch-off.

- (1) A
- (2) B
- (3) C
- (4) D
- **16.** Assertion:— A small magnet takes longer time in falling in a hollow metrallic tube without touching the wall.

**Reason:** There is opposition of motion due to production of eddy currents in metallic tube.

- (1) A
- (2) B
- (3) C
- (4) D
- 17. In shown circuit switch is closed at t = 0.



**Assertion:** At t = 0, current through battery

 $I = \frac{E}{2R} \text{ and at } t = \infty, \text{ current through battery will}$ 

be  $I = \frac{E}{R}$ .

**Reason:** At t = 0, inductor will behave like open circuit and at  $t = \infty$ , inductor will behave like short circuit.

- (1) A
- (2) B
- (3) C
- (4) D

- **18. Assertion:**—Inductance coil are made of copper. **Reason:** Copper has a very small ohmic resistance.
  - (1) A
- (2) B
- (3) C
- (4) D
- **19. Assertion:** An emf is induced in long solenoid by a small bar magnet that moves while totally inside it along the solenoid axis.

**Reason:** As the magnet moves inside the solenoid, the flux through individual turns of the solenoid does not change.

- (1) A
- (2) B
- (3) C
- (4) D
- **20. Assertion:**—The coils in the resistance boxes are made by doubling the wire.

**Reason:**— When two coils are wound on each other, the mutual inductance is zero.

- (1) A
- (2) B
- (3) C
- (4) D
- **21. Assertion** :- Induced electric field is non conservative.

**Reason** :-  $\oint \vec{E}.d\vec{\ell} \neq 0$ 

- (1) A
- (2) B
- (3) C
- (4) D
- **22.** Assertion: Induced electric field lines form closed loops in space.

**Reason:** Induced electric field lines do not originate & terminate at charged particle.

- (1) A
- (2) B
- (3) C
- (4) D
- **23**. **Assertion**: In L-R circuit, if higher value of L is taken then it will take more time to reach steady state value of current.

**Reason:** For higher value of L, back emf is larger.

[AIIMS 2015]

- (1) A
- (2) B
- (3) C
- (4) D
- **24. Assertion**: MRI is an excellent method to find problem in internal tissues. [AIIMS 2016]

**Reason:** Two third of the human body is made up of hydrogen which has one electron.

- (1) A
- (2) B
- (3) C
- (4) D
- **25. Assertion :-** In a step down transformer, value of voltage in secondary coil is less than in primary. **Reason :-** Linked magnetic flux in secondary is

**Reason**:- Linked magnetic flux in secondary is less than in primary. [AIIMS 2016]

- (1) A
- (2) B
- (3) C
- (4) D



**26. Assertion**: In higher power transmission, 240 V is preferred over 120 V.

**Reason:** Power loss is more in case of 120 V as compared to 240 V. **[AIIMS 2016]** 

- (1) A
- (2) B
- (3) C
- (4) D
- **27. Assertion**: In an R-L circuit if current is increasing then inductor behave as a conducting wire.

[AIIMS 2017]

**Reason**:- In steady state, current in L-R circuit is independent of L.

- (1) A
- (2) B
- (3) C
- (4) D

EX	ERC	SE-II	(Ass	ertion	& Re	ason)							ANS	WER	KEY
Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	2	1	1	2	2	3	3	1	2	2	1	3	1	4	1
Que.	16	17	18	19	20	21	22	23	24	25	26	27			
Ans.	1	1	1	4	3	1	1	1	3	1	1	4			

